

# Assessing complex route choice models using an abstracted network based on mental representations

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# Agenda

- 1 Context
- 2 Route choice with mental representations
- 3 Analysis
- 4 Conclusion

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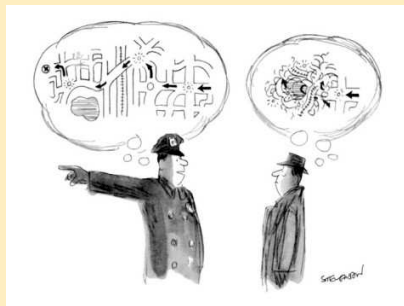
# Route choice modeling

## Operational difficulties

- Data
- Choice set
- Structural correlation



## Behavioral aspect



# The MRI approach

How can we represent a route in a behaviorally realistic way without increasing the model complexity?

→ Model the **strategic** decisions of people instead of the *operational* ones.

✓ **Mental Representation Item (MRI)** → short description of a route

Kazagli, E., Bierlaire, M., and Flötteröd, G. (2016). Revisiting the Route Choice Problem: A Modeling Framework Based on Mental Representations, *Journal of Choice Modelling* 19:1-23. doi:10.1016/j.jocm.2016.06.001



# Objectives

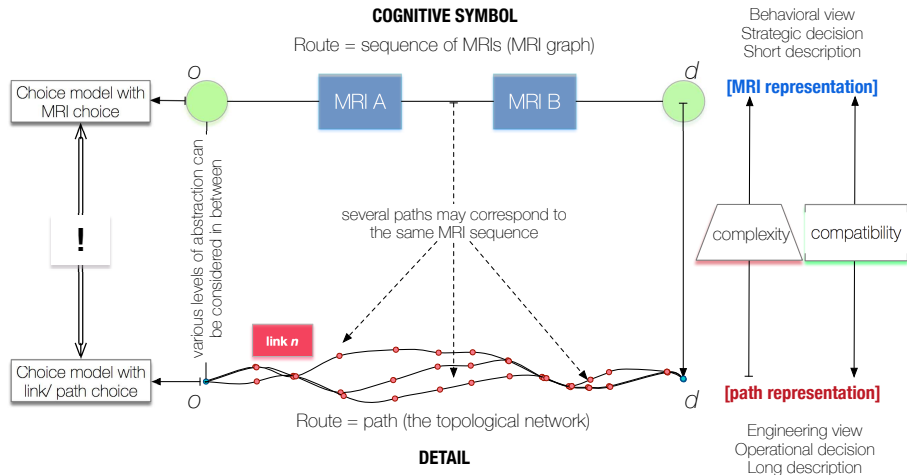
*Current work and way forward*

Potential of the MRI approach in:

- ❶ simplifying and assessing complex route choice models
  - Recursive logit (RL) [Fosgerau et al., 2013]; [Mai et al., 2015]
  - Error components (EC) [Frejinger and Bierlaire, 2007]
  - Cross-nested logit (CNL) [Vovsha and Bekhor, 1998]; [Lai and Bierlaire, 2015]
- ❷ improving route guidance and map design
  - cognitive limits in “megacities”
  - information provision for navigation in multilayer transportation systems

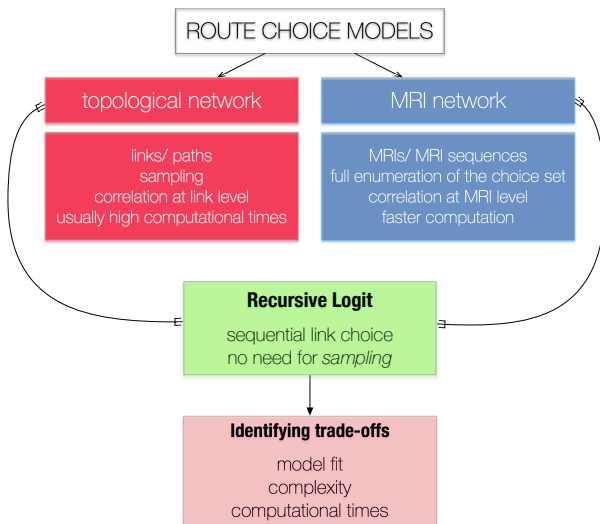
# Hierarchical structure and consistency

*From MRIs to paths and vice versa*



# Goal

## *Specification and estimation using real data*



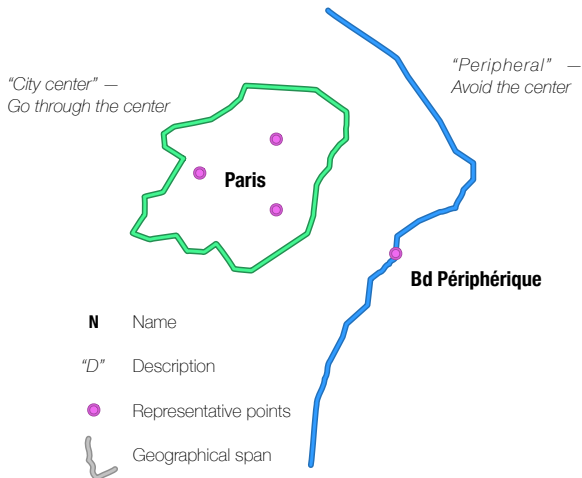


# Agenda

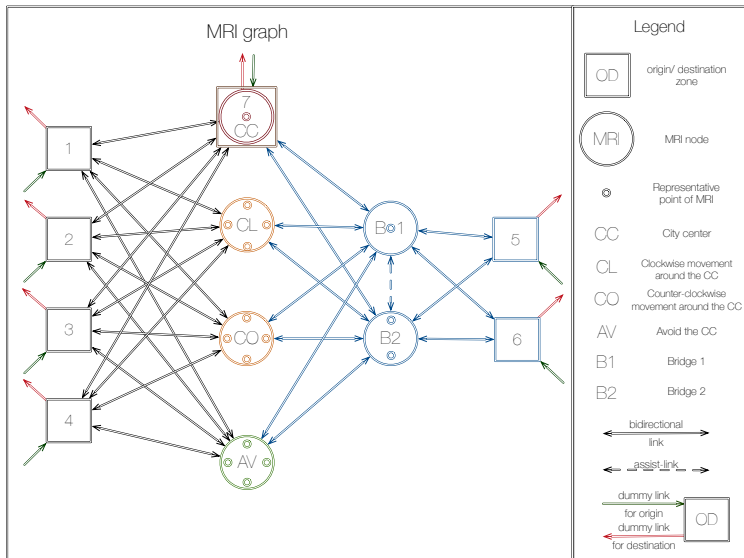
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# Recap MRI definition

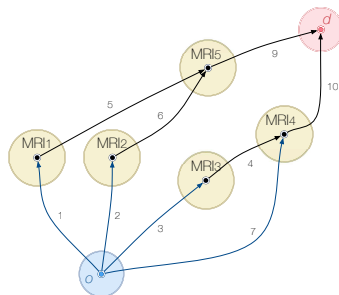
Conceptual: a name and a description; Operational: a point and a span



# Blueprint of a MRI network for route choice



# EC model with MRIs

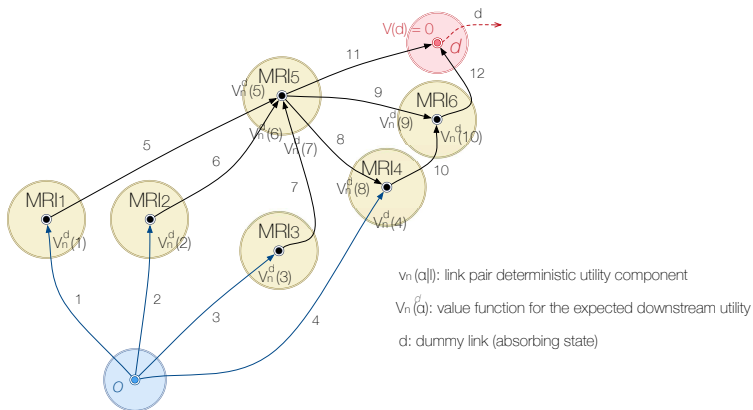


- Each MRI is associated with an error component.
- An alternative  $i$  is correlated with alternative  $j$  if they use the same MRI.

This is similar to the subnetwork approach proposed by [Frejinger and Bierlaire, 2007], but the MRIs are also the building blocks of the alternatives in the choice set.

# RL model on the MRI graph

As soon as the MRI network is defined it is trivial to apply the formulation proposed by [Fosgerau et al., 2013] for the RL model.



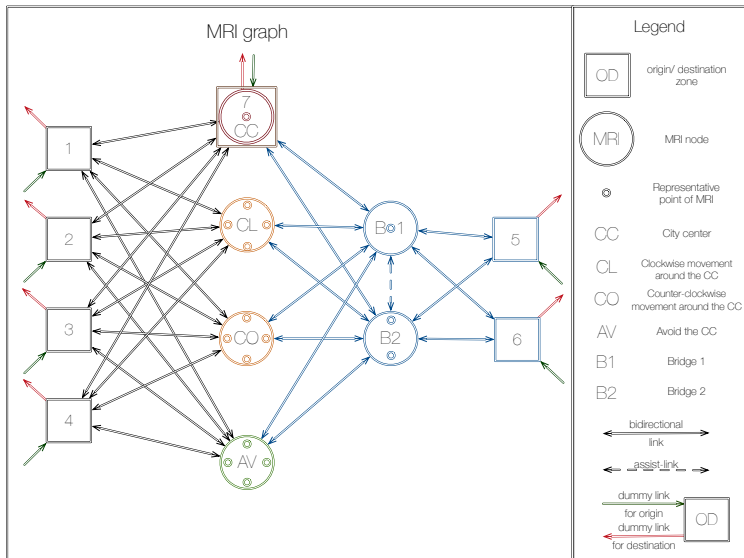
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# Borlänge dataset

- ➊ GPS data → map-matched trajectories
- ➋ Borlänge road network:
  - ➊ 3077 nodes and 7459 unidirectional links
  - ➋ Link travel times
- ➌ We identified 6 MRIs.
- ➍ We use a sample of 239 observations.

# Borlänge MRI network





# Analysis

model type	MRI	path
MNL	✓	—
RL	✓	✓
EC	✓	—

## 1 Model output

- Probabilities
- Elasticities
- Ratios of parameters

## 2 Model application

- Link flows

## 3 Computational times

# Specification table

Parameter name	Model 1 MNL/ RL with MRIs <sup>1</sup>	Model 2 EC with MRIs	Model 3 RL with paths
$ASC_{AVOID}$	1	1	1
$ASC_{CC}$	1	1	1
$ASC_{BRIDGE1}$	1	1	1
$\beta_{TIME}$	TT <sup>2</sup> (min)	TT (min)	TT (min)
$\beta_{IS}$	# intersections	# intersections	# intersections
$\beta_{LT}$	# left turns	# left turns	# left turns
$\omega_{AVOID}$	×	$\sim \mathcal{N}(0, \sigma_{AVOID}^2)$	×
$\omega_{CC}$	×	$\sim \mathcal{N}(0, \sigma_{CC}^2)$	×
$\omega_{BRIDGE1}$	×	$\sim \mathcal{N}(0, \sigma_{BRIDGE1}^2)$	×

<sup>1</sup>The RL model is equivalent to the MNL with full choice set for a cycle-free network.

<sup>2</sup>TT: travel time

# Estimation results

Parameter name	Model 1: MNL with MRIs Parameter value; (Rob. t-test 0)	Model 2: EC with MRIs Parameter value; (Rob. t-test 0)	Model 3: RL with paths Parameter value; (t-test 0)
$ASC_{AVOID}$	1.69; (5.51)	2.25; (5.24)	0.087; (1.98)
$ASC_{CC}$	-2.07; (-3.96)	-6.38; (-1.11)	-0.179; (-5.10)
$ASC_{BRIDGE1}$	-1.93; (-5.01)	-4.14; (-2.93)	0.615; (1.61)
$\beta_{TIME}$	-0.474; (-14.94)	-0.596; (-13.86)	-2.420; (-14.56)
$\beta_{IS}$	-0.041; (-1.45)	-0.115; (-3.01)	-0.407; (-7.64)
$\beta_{LT}$	-0.076; (-1.50)	-0.104; (-1.58)	-0.975; (-18.98)
$\omega_{AVOID}$	-	2.05; (3.46)	-
$\omega_{CC}$	-	3.96; (1.24)	-
$\omega_{BRIDGE1}$	-	4.59; (2.17)	-
<b>Number of observations</b>	239	239	239
<b>Number of parameters</b>	6	9	6
<b>Number of draws</b>	-	1000	-
$\mathcal{L}(0)$	-619.617	-629.983	
$\mathcal{L}(\hat{\beta})$	-193.633	-183.558	1565.49

# Ratios of parameters

Model	$\beta_{TIME}$	$\beta_{IS}$	$\beta_{LT}$	$\beta_{IS}/\beta_{TIME}$	$\beta_{LT}/\beta_{TIME}$	$\beta_{IS}/\beta_{LT}$
MNL/ RL	-0.474	-0.041	-0.076	0.086	0.161	0.536
RL (paths)	-2.420	-0.407	-0.975	0.168	0.403	0.418
EC	-0.596	-0.115	-0.104	0.193	0.174	1.106

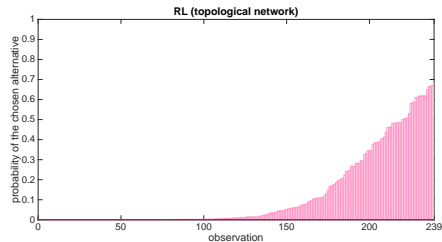
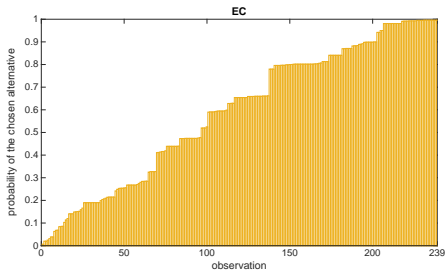
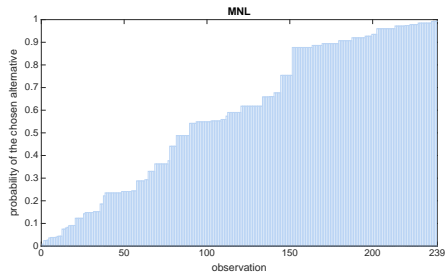
Model	CC	AVOID	BRIDGE1	AVOID/ CC	BRIDGE1/ CC	AVOID/ BRIDGE1
MNL/ RL	-2.070	1.690	-1.930	-0.816	0.932	-0.876
RL (paths)	-0.179	0.087	0.615	-0.487	-3.440	0.142
EC	-6.380	2.250	-4.140	-0.353	0.649	-0.543

Model	$\beta_{TIME}$	CC	AV	BRIDGE1	CC/ $\beta_{TIME}$	AV/ $\beta_{TIME}$	BRIDGE1/ $\beta_{TIME}$
MNL/ RL	-0.474	-2.070	1.690	-1.930	4.368	-3.565	4.072
RL (paths)	-2.420	-0.179	0.087	0.615	0.074	-0.036	-0.254
EC	-0.596	-6.380	2.250	-4.140	10.705	-3.775	6.946

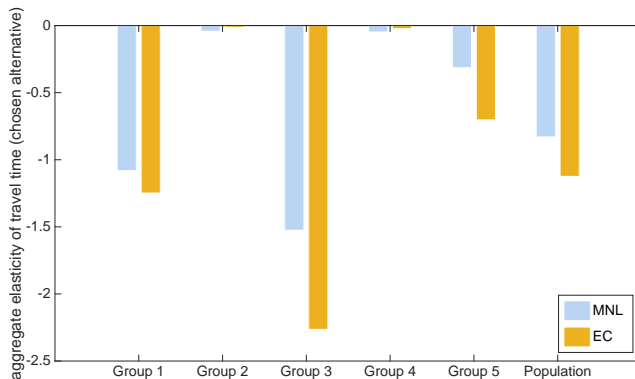
# Computational times

<b>Model</b>	<b>MRI representation</b>	<b>path representation</b>
<b>MNL</b>	0 min	—
<b>RL</b> (with ASCs)	0 (2) min	~ 20 (45) min
<b>EC</b>	~ 60 min	—

# Probability of the chosen alternative

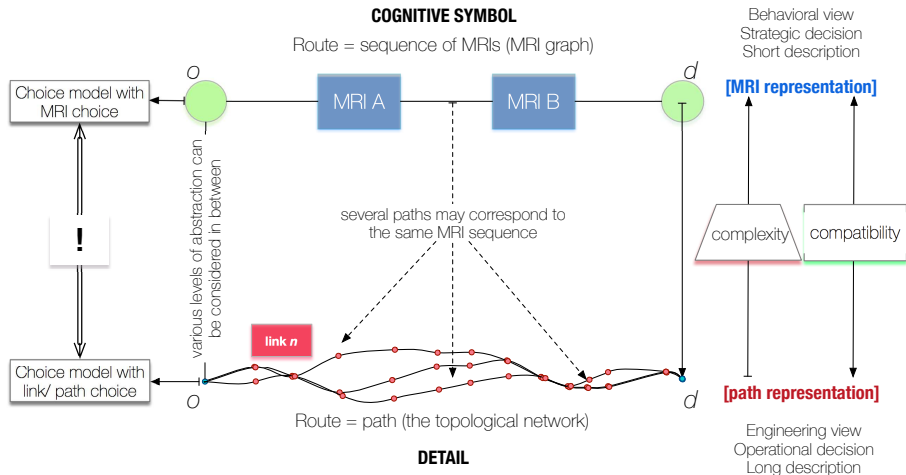


# Aggregate elasticity of travel time (chosen alternative)



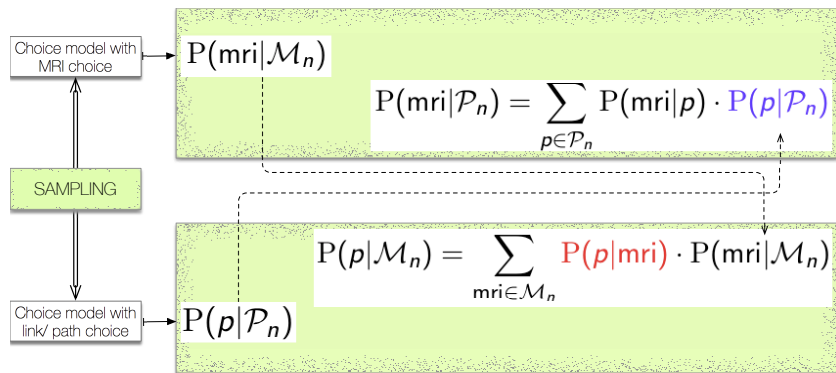
# Hierarchical structure and consistency

*From MRIs to paths and vice versa*





# Comparing aggregate and disaggregate output



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# Conclusion

- Exploiting behavioral rationale to facilitate the estimation and application of route choice models to large networks.
  - 1 MNL as a benchmark.
  - 2 RL: MRI approach to reduce the state space.
  - 3 EC: MRI approach to capture perceptual correlation.
  - 4 CNL: MRI approach to reduce the number of nests.
- Aggregate/ disaggregate approach.
  - Can we obtain a similar result?

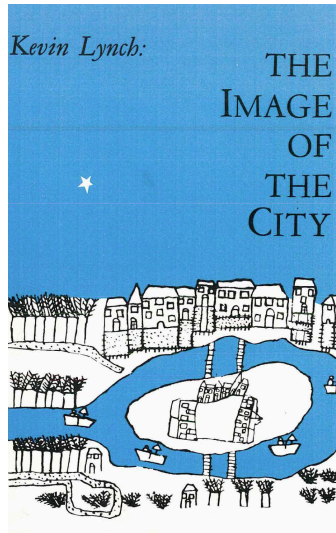
# Future work

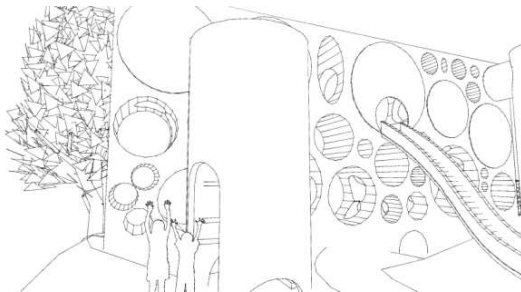
- ❶ Test the MRI approach in a large network and dataset.
  - How complicated it is to define a realistic and operational MRI network for a very big, complex topological network?
- ❷ Relevance for route guidance and map design.
  - [Gallotti et al., 2016] Lost in transportation: Information measures and cognitive limits in multilayer navigation.

## Mapping, Beirut-style: how to navigate a city without using any street names.

*Jenny Gustafsson in Beirut, for The Guardian (June, 2015)*

*"It is about learning how a city works. There is usually a very clear order; you just have to understand it. Once you know this, navigation is not hard. ... references and directions like 'nearby', 'opposite' and 'in between', because roads often have no signs. ... creative names like "The Road with the Oak Tree" ..."*





Thank you!

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# Bibliography



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A link based network route choice model with unrestricted choice set.  
*Transportation Research Part B: Methodological*, 56(0):70 – 80.



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*Transportation Research Part B: Methodological*, 41(3):363–378.



Gallotti, R., Porter, M. A., and Barthelemy, M. (2016).  
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*Science Advances*, 2(2).



Lai, X. and Bierlaire, M. (2015).  
Specification of the cross-nested logit model with sampling of alternatives for route choice models.  
*Transportation Research Part B: Methodological*, 80:220 – 234.



Mai, T., Fosgerau, M., and Frejinger, E. (2015).  
A nested recursive logit model for route choice analysis.  
*Transportation Research Part B: Methodological*, 75:100 – 112.



Vovsha, P. and Bekhor, S. (1998).  
Link-Nested Logit Model of Route Choice: Overcoming Route Overlapping Problem.  
*Transportation Research Record: Journal of the Transportation Research Board*, 1645:133–142.

# The MRI network

*For a given case study & scope of analysis*

- 1 Define the MRIs and the origin  $o$  and destination  $d$  zones.
- 2 For each MRI  $r$  create a node.
- 3 For each  $o$  and  $d$  zone determine the centroid  $s$  of the zone and create a node corresponding to it.

The number of vertices of the MRI network equals the summation of the number of MRIs  $\mathcal{R}$  and zone centroids  $\mathcal{S}$ .

- 4 For each pair of nodes in the MRI network create a link (edge)  $\ell$  if the transition from one node to another is allowed.

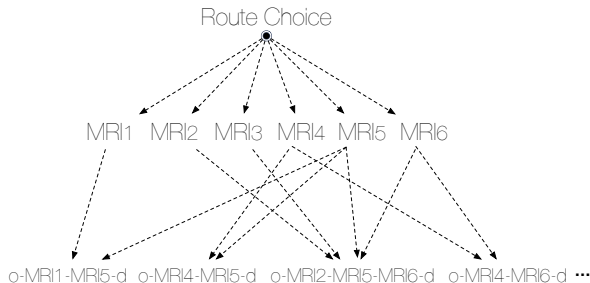


## Recap Definition of alternatives

Following the definition of the MRI, a route is defined as:

- 1 an origin,
- 2 an ordered sequence of MRIs (possibly only one), and
- 3 a destination.

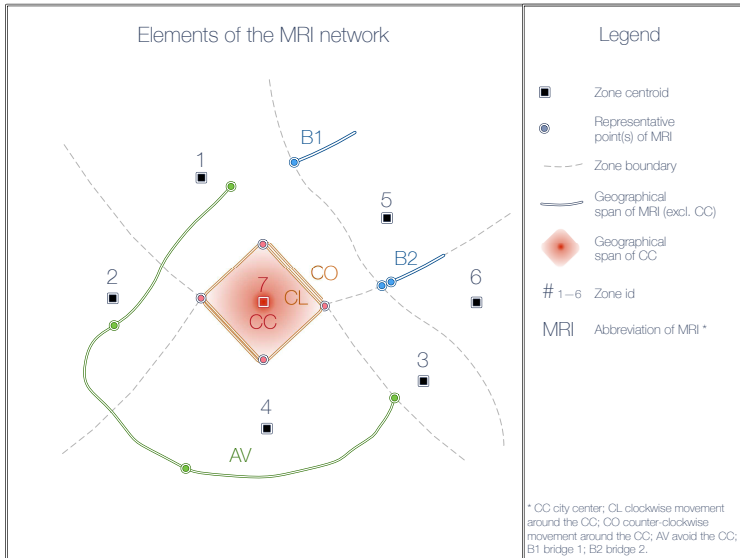
# CNL model with MRIs



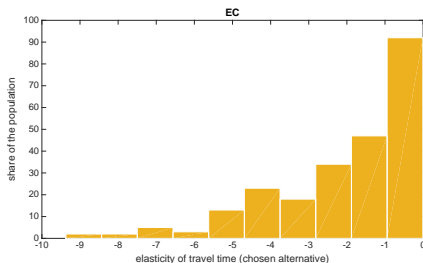
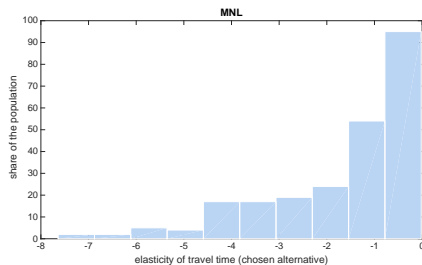
- Each MRI is a nest.
- An alternative  $i$  belongs to nest  $m$  if MRI  $m$  appears in the sequence  $i$ .

This is similar to [Vovsha and Bekhor, 1998] and [Lai and Bierlaire, 2015], but nests correspond to MRIs instead of links.

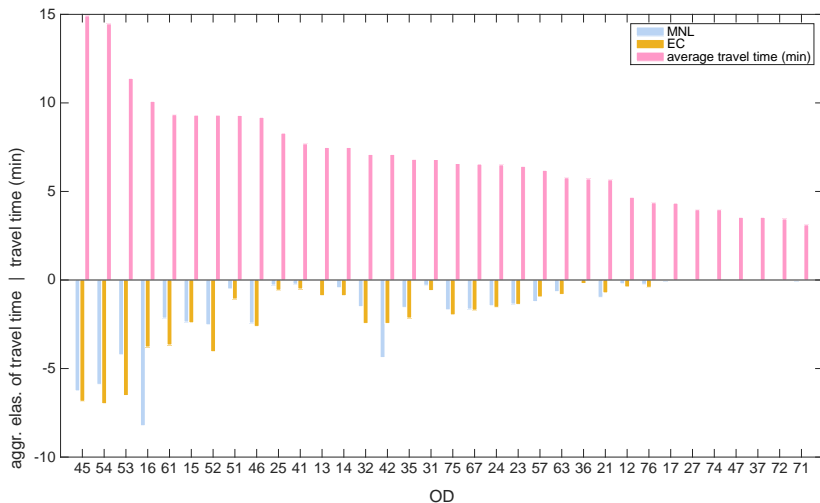
# Borlänge MRI components



# Elasticity of travel time (chosen alternative)



# Aggregate elasticity of travel time (chosen alternative)

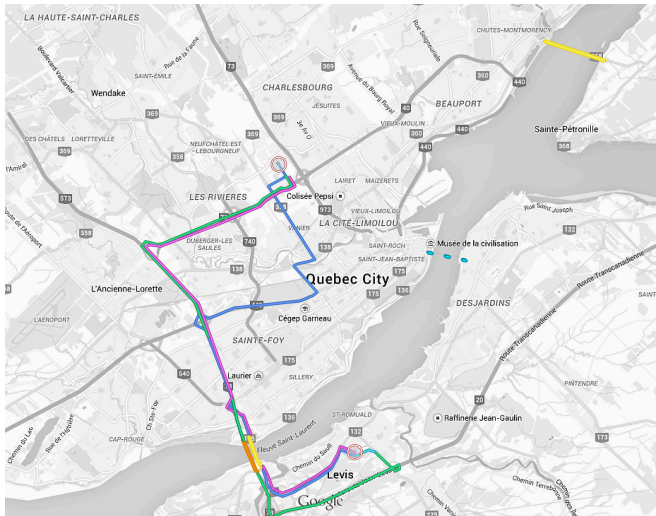


# Québec dataset

- ① Smartphone data collection → more than 20000 GPS trajectories
  - ✓ Departure times
  - ✓ Trip purposes
  - ✓ Land use information
- ② Quebec road network:
  - ~ 20000 nodes and 40000 unidirectional links

# Québec

## *Autoroutes and bridges*



# Québec

## *Bridge vs ferry boat*

