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Assessing complex route choice models using an abstracted network based on mental representations

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Route choice with MRIs





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Route choice modeling



(\cdot) Data

Choice set generation



Image: Image:

Context

Recent advances

Fosgerau et al., 2013] Recursive logit (RL)

- Sequential link choice in a dynamic framework.
- Avoids full enumeration.
- No need for sampling.

Further extended by [Mai et al., 2015] to the nested RL.

- [Lai and Bierlaire, 2015] Cross-nested logit (CNL) with sampling of alternatives
 - Avoids full enumeration.
 - Metropolis-Hastings for route choice proposed by [Flötteröd and Bierlaire, 2013].
 - Sepansion factor inspired by [Guevara and Ben-Akiva, 2013].

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The MRI approach

How can we represent a route in a behaviorally realistic way without increasing the model complexity?

- \rightarrow Model the strategic decisions of people instead of the operational ones.
- ✓ Mental Representation Item (MRI)

Kazagli, E., Bierlaire, M., and Flötteröd, G. (2015). Revisiting the Route Choice Problem: A Modeling Framework Based on Mental Representations. Technical report TRANSP-OR 150824. Transport and Mobility Laboratory, ENAC. EPFL.



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Current work Objective

Potential of the MRI approach in simplifying complex route choice models:

- RL
- \bigcirc EC¹
- 3 CNL
- \rightarrow Identify the trade-offs:
 - model fit
 - complexity
 - computational time

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¹Error components

Current work Goal

Specification and comparison using real data

model type	MRI	path
MNL ²	\checkmark	_
RL	\oplus	\checkmark
EC	\checkmark	_
CNL	\oplus	_

² Multinomial	logit
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MRI example in Aruba



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Recap The MRI definition

Conceptual: a name and a description; Operational: a point and a span



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Recap Definition of alternatives

Following the definition of the MRI, a route is defined as:

- an origin,
- an ordered sequence of MRIs (possibly only one), and
- a destination.

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The MRI network

For a given case study & scope of analysis

- **①** Define the MRIs and the origin o and destination d zones.
- **2** For each MRI r creat a node.
- For each o and d zone determine the centroid s of the zone and create a node corresponding to it.

The number of vertices of the MRI network equals the summation of the number of $\mathrm{MRIs}\ \mathcal{R}$ and zone centroids $\mathcal{S}.$

● For each pair of nodes in the MRI network create a link (edge) l if the transition from one node to another is allowed.

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RL model with MRIs

As soon as the MRI network is defined it is trivial to apply the formulation proposed by [Fosgerau et al., 2013] for the RL model.



EC model with MRIs



- Each MRI is associated with an error component.
- \bullet An alternative i is correlated with alternative j if they use the same MRI.

This is similar to the subnetwork approach proposed by [Frejinger and Bierlaire, 2007], but the MRIs are also the building blocks of the alternatives in the choice set.

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CNL model with MRIs



- Each MRI is a nest.
- \bullet An alternative i belongs to nest m if MRI m appears in the sequence i.

This is similar to [Vovsha and Bekhor, 1998] and [Lai and Bierlaire, 2015], but nests correspond to MRIs instead of links.

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Route choice with MRIs





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Borlänge dataset

- 2 Borlänge road network:
 - 3077 nodes and 7459 unidirectional links
 - 2 Link travel times
 - Olear choices
- **3** We identified 6 MRIs.
- We use a sample of 239 observations.

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Borlänge MRI network elements



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Borlänge MRI network



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Analysis

model type	MRI	path
MNL	\checkmark	_
RL	\oplus	\checkmark
EC	\checkmark	_
CNL	\oplus	_

- Direct comparison
 - Probabilities
 - Elasticities
 - Ratios of parameters
- Indirect comparison
 - Link flows
- Computational times

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Specification table

Parameter name	Model 1Model 2nameMNL with MRIsEC with MRIs		Model 3 RL with paths	
ASC _{AVOID} ASC _{CC} ASC _{BRIDGE1}	1 1 1	1 1 1	× × ×	
$eta_{ extsf{time}}$	TT ³ (min)	TT (min)	TT (min)	
$eta_{\it IS}$	# intersections	# intersections	# intersections	
β_{LT}	# left turns	# left turns	# left turns	
ω _{AVOID} ω _{CC} ω _{BRIDGE1}	× × ×	$egin{aligned} &\sim \mathcal{N}(0, \sigma^2_{AVOID}) \ &\sim \mathcal{N}(0, \sigma^2_{CC}) \ &\sim \mathcal{N}(0, \sigma^2_{BRIDGE1}) \end{aligned}$	× × ×	

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Estimation results

Parameter name	Model 1: MNL with MRIs Parameter value; (Rob. t-test 0)	Model 2: EC with MRIs Parameter value; (Rob. t-test 0)	Model 3: RL with paths Parameter value; (t-test 0)	
ASC _{AVOID}	1.69; (5.51)	2.25; (5.24)	-	
ASC _{CC}	-2.07; (-3.96)	-6.38; (-1.11)	-	
ASC _{BRIDGE1}	-1.93; (-5.01)	-4.14; (-2.93)	-	
β_{TIME}	-0.474; (-14.94)	-0.596; (-13.86)	-3.735; (-15.91)	
β_{IS}	-0.041; (-1.45)	-0.115; (-3.01)	-0.322; (-3.86)	
β_{LT}	-0.076; (-1.50)	-0.104; (-1.58)	-1.035; (-36.16)	
ω_{AVOID}	-	2.05; (3.46)	-	
ω _{CC}	-	3.96; (1.24)	-	
$\omega_{BRIDGE1}$	-	4.59; (2.17)	-	
Number of observations	239	239	239	
Number of parameters	6	9	3	
$\mathcal{L}(0)$	-619.617	-629,983	-	
$\mathcal{L}(\hat{\beta})$	-193.633	-183.558	10.992	

Ratios of parameters

Model	β_{TIME}	β_{IS}	β_{LT}	$\beta_{\text{IS}}/\beta_{\text{TIME}}$	β_{LT}/β_{TIME}	β_{IS}/β_{LT}
MNL	-0.474	-0.0408	-0.0761	0.086	0.161	0.536
RL	-3.735	-0.322	-1.035	0.086	0.277	0.311
EC	-0.596	-0.115	-0.104	0.193	0.174	1.106

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Computational times

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Model	MRI representation	path representation
MNL	0 min	_
RL	?	\sim 20 min
EC	\sim 60 min	_

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Probability of the chosen alternative



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Elasticity of travel time (chosen alternative)



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Aggregate elasticity of travel time (chosen alternative)



Aggregate elasticity of travel time (chosen alternative)



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Conclusion

- Exploiting behavioral rationale to facilitate the estimation and application of route choice models to large networks.
 - MNL as a benchmark.
 - **2** EC: MRI approach to capture perceptual correlation.
 - In RL: MRI approach to reduce the state space.
 - ONL: MRI approach to reduce the number of nests.
- Comparison under the MRI approach.

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Future work



- City of Québec.
- More than 20000 GPS trajectories.
- Relevance for route guidance and map design.
 - [Gallotti et al., 2016] Lost in transportation: Information measures and cognitive limits in multilayer navigation.

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Mapping, Beirut-style: how to navigate a city without using any street names.

Jenny Gustafsson in Beirut, for The Guardian (June, 2015)

"It is about learning how a city works. There is usually a very clear order; you just have to understand it. Once you know this, navigation is not hard references and directions like 'nearby', 'opposite' and 'in between', because roads often have no signs. ... creative names like "The Road with the Oak Tree"..."



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Thank you!

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Appendix

The MRI network

Blueprint example



From MRIs to paths



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Québec dataset

- Smartphone data collection \rightarrow more than 20000 GPS trajectories
 - ✓ Departure times
 - \checkmark Trip purposes
 - \checkmark Land use information
- Quebec road network:
 - ~ 20000 nodes and 40000 unidirectional links

Image: Image:

Québec

Autoroutes and bridges



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Québec

Bridge vs ferry boat



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