# Freight Railway Network Design Problem

Nikola Obrenović, Virginie Lurkin, Michel Bierlaire Transport and Mobility Laboratory TRANSP-OR École Polytechnique Fédérale de Lausanne EPFL

> Vincent J. Baeriswyl, Jasmin Bigdon SBB Cargo AG, Olten, Switzerland

OR Days 2018, Bern, Switzerland





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## Marshaling and shunting yards

• Bundling different commodities with close origins and destinations



#### **Problem setting**

- Existing SBB Cargo network
  - 2 inner marshaling yards
  - 3 border marshaling yards
  - Approx. 70 shunting yards 50 can be changed
- Determine optimal number and locations of the yards









#### **Related** problems

- Hub location problem (HLP)
  - Missing track capacities and hub operation costs
- Multicommodity flow problem (MFP)
  - Missing hub capacities and operation costs
- Multicommodity network design problem (MNDP)
  - Missing hub types and operation costs





#### Problem definition

- Extension of the arc-node formulation of the MFP
- Network elements:
  - N Set of stations, including potential marshaling and shunting yards
  - A Set of direct, existing links between the stations
  - B Set of added direct links between the yards
  - K Set of transported commodities each described with the origin, destination, weight and number of wagons





• Additional arcs to model transport of bundled commodities



- Inner node arcs to model different station types
  - Only one can be used
  - Shunting capacity as the inner arc capacity







• Objective function:

$$\min \sum_{k \in K} \sum_{(i,j) \in A \cup B} c_{ij}^k x_{ij}^k + \sum_{k \in K} \sum_{i \in N} Sv^k s_i^k + \sum_{k \in K} \sum_{i \in N} Mv^k m_i^k$$

- Constants:
  - $c_{ij}^k$  Cost of transporting commodity k via arc (i, j)
  - $v^k$  Number of wagons of commodity k
  - S Cost of shunting one wagon in a shunting yard
  - M Cost of shunting one wagon in a marshaling yard
- Variables:
  - $x_{ij}^k$  Determines if commodity k is transported via arc (i, j)
  - $s_i^k$  Determines if commodity k is shunted in the shunting yard i
  - $m_i^k$  Determines if commodity k is shunted in the marshaling yard i





• Node type constraints:

$$\begin{split} &\sum_{k \in K} r_i^k \leq r_i \mathcal{M}_1, \qquad \forall i \in N \\ &\sum_{k \in K} s_i^k \leq s_i \mathcal{M}_2, \qquad \forall i \in N \\ &\sum_{k \in K} m_i^k \leq m_i \mathcal{M}_3, \qquad \forall i \in N \\ &r_i + s_i + m_i = 1, \qquad \forall i \in N \end{split}$$

• Arc usage constraints:

- Variables:
  - r<sub>i</sub> Equals to 1 if i is a regular station, otherwise equals to 0
  - $s_i$  Equals to 1 if i is a shunting yard, otherwise equals to 0
  - $m_i$  Equals to 1 if i is a marshaling yard, otherwise equals to 0

$$2x_{ij}^k \le s_i^k + m_i^k + s_j^k + m_j^k, \qquad \forall (i,j) \in B, \forall k \in K$$





• Inner arc capacity constraints:

$$\sum_{k \in K} v^k (r_i^k + s_i^k + m_i^k) = d_i, \qquad \forall i \in N$$

$$d_i \leq r_i \mathcal{M} + s_i C_S + m_i C_M, \qquad \forall i \in N$$

- Constants:
  - $C_S$  Maximum capacity of a shunting yard
  - $C_M$  Maximum capacity of a marshaling yard
- Variables:
  - $d_i$  Required capacity of the node i





- Size of the SBB Cargo network:
  - Approx. 2100 stations
  - Approx. 2500 direct links
- Over 65000 commodities
  - Yearly demand, scaled to daily average





#### Heuristic algorithm

- Hub location:
  - Adaptive large neighborhood search
  - Variable neighborhood search



#### Heuristic algorithm - Neighborhoods



• Select the busiest station close to the MY and exchange their locations



• Select the least used MY and convert it into SY



• Select SY with fully utilized, maximum capacity and convert it into MY





#### Heuristic algorithm - Neighborhoods



• Select SY with most unused capacity and decrease it



• Select SY with fully utilized, below-maximum capacity and increase it





#### Heuristic algorithm - Neighborhoods

# SY $\rightarrow$ ST

• Select underused SY with minimum capacity and convert it into a regular station



• Select frequently used regular station and convert it into a SY with minimum capacity





### Heuristic algorithm

- Commodity routing:
  - Prioritized assignment algorithm







#### Heuristic algorithm - Path alternatives

- Direct (shortest) path
  - Unbundled commodity

- Via marshaling yards
  - Bundled commodity





#### Heuristic algorithm - Path alternatives

- Via shunting yards
  - Bundled commodity
- Via one marshaling and one shunting yard
  - Bundled commodity





- Developed algorithm is very flexible:
  - Easily extendable with additional neighborhood operators, i.e. network transformations
  - Easy definition of specific initial network states, e.g. all marshaling yards closed, several additional marshaling yards open, etc.





- Network states with potential transportation cost reduction identified with two strategies (thus far):
  - I. SI: Allowing opening of new marshaling yards
  - 2. S2: Disallowing opening of new marshaling yards





# Preliminary results (cont.)

• Best resulting networks:

Strat.	New MY	Rem. MY	Mov. MY	Total MY	New SY	Rem. SY	Total SY	Cost reduct.
Orig. net.	-	-	-	2	-	-	50	-
S1	3	0	0	5	0	4	46	8.505%
S2	0	1	1	1	19	5	64	1.857%

- Daily transportation cost in the original network: over 38 Million CHF
- Running time: approx. 9h





#### **Results discussion**

- Costs of transportation are dominant over yard operation costs
- Cost of yard maintenance is not taken into account
  - This cost contributes to reducing the number of yards and their size
  - Opening new yards will be less favored by the algorithm
  - Could be included in another case study
- New yards can be near the existing ones
  - E.g. in SI, new MY Territet is opened close to Lausanne MY
  - The objective function should penalize this situation





#### Conclusions

- Developed algorithm explores various network changes, their combinations and their influence to the transportation costs
  - Flexible, easily extendable algorithm
- The algorithm identified network changes resulting in transportation cost reduction
- The objective function should be extended with the real **costs of maintenance** of the marshaling and shunting yards
  - Relevant change in the algorithm result





- Include penalty for having two yards near each other
- Include trains in the model formulation and heuristic
- Solve the problem exactly on the subset of input data
  - To benchmark the heuristic result







# Questions? nikola.obrenovic@epfl.ch





#### References

- C. Barnhart, N. Krishnan and P. H. Vance: Multicommodity Flow Problems. In Encyclopedia of Optimization, C.A. Floudas and P. M. Pardalos (eds), vol. 14, 2354-2362, Springer, 2009.
- R. Z. Farahani, M. Hekmatfar, A. B. Arabani and E. Nikbakhsh: *Hub location*
- problems: A review of models, classication, solution techniques, and applications.
  Computers & Industrial Engineering 64, 1096-1109, 2013.
- S. Ropke and D. Pisinger: An adaptive large neighborhood search heuristic for the pickup and delivery problem with time windows. Transportation Science 40, 455-472, 2006.
- S. Binder, Y. Maknoon and M. Bierlaire: Exogenous priority rules for the capacitated passenger assignment problem. Transportation Research Part B: Methodological 105, 19-42, 2017.



