# Capacity-Oriented Marshaling and Shunting Yards Location Problem

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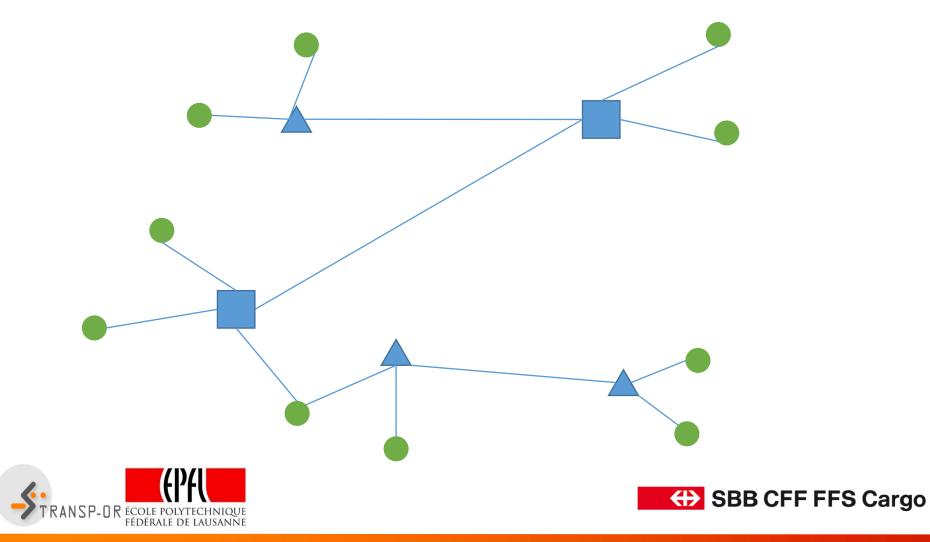
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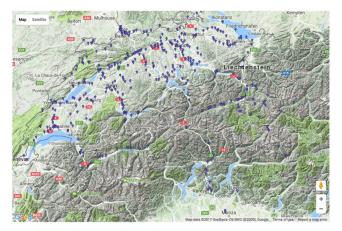
## Marshaling and shunting yards

• Bundling different commodities with close origins and destinations



## **Problem setting**

- Existing SBB Cargo network
  - 2 inner marshaling yards
  - 3 border marshaling yards
  - Approx. 70 shunting yards 50 can be changed
- Determine optimal number and locations of the yards









## **Related** problems

- Hub location problem (HLP)
  - Missing track capacities and hub operation costs
- Multicommodity flow problem (MFP)
  - Missing hub capacities and operation costs
- Multicommodity network design problem (MNDP)
  - Missing hub types and operation costs





- Extension of the HLP
- Network elements:
  - N Set of stations, including potential marshaling and shunting yards
  - A Set of direct links between the stations
  - K Set of transported commodities each described with the origin, destination, weight and number of wagons





## Problem definition (cont.)

- Constants:
  - $d_{ij}$  Shortest distance between nodes i and j
  - $k_o$  Origin of commodity k
  - $k_d$  Destination of commodity k
  - $w^k$  Weight of commodity k
  - $P_W$  Cost of transporting a weight unit of any commodity per distance unit
  - $P_D$  Cost of the locomotive and driver per distance unit
  - $v^k$  Number of wagons of commodity k
  - $V_{max}$  Maximum number of wagons in a train
  - S Cost of shunting one wagon in a shunting yard
  - M Cost of shunting one wagon in a marshaling yard





- Transportation cost per distance unit:
  - Unbundled commodity:

$$c^k = w^k P_W + P_D \qquad \forall k \in K$$

• Bundled commodity:

$$c_r^k = w^k P_W + \frac{v^k}{V_{max}} P_D \qquad \forall k \in K$$





• Objective function:

$$\min \sum_{k \in K} \left( \sum_{i \in N} \sum_{j \in N} X_{ij}^{k} \left( \left( d_{ik_{o}} + d_{jk_{d}} \right) c^{k} + d_{ij} c_{r}^{k} + (s_{i}S + m_{i}M + s_{j}S + m_{j}M) v^{k} \right) + (1 - z^{k}) d_{k_{o}k_{d}} c^{k} \right)$$

- Variables:
  - $X_{ij}^k$  Determines if commodity k is transported via hubs i and j
  - $s_i$  Determines if the node i is a shunting yard
  - $m_i$  Determines if the node i is a marshaling yard
  - $z^k$  Determines if the commodity k is transported bundled





## Problem definition (cont.)

• Node type constraints:

$$r_i + s_i + m_i = 1$$
,  $\forall i \in N$ 

• Commodity shunting constraints:

$$\sum_{i \in N} \sum_{j \in N} X_{ij}^k = z^k, \qquad \forall k \in K$$

$$2X_{ij}^k \le s_i + m_i + s_j + m_j, \qquad \forall k \in K, \forall i \in N, \forall j \in N$$





## Problem definition (cont.)

• Node capacity constraints:

$$\begin{split} \sum_{k \in K} \sum_{j \in N} X_{ij}^k v^k + \sum_{k \in K} \sum_{j \in N} X_{ji}^k v^k &= a_i, \quad \forall i \in N \\ a_i &\leq r_i \mathcal{M} + s_i C_S + m_i C_M, \quad \forall i \in N \end{split}$$

Variables:

•  $a_i$  – Required capacity of the node i

Constants:

- $\mathcal{M}$  Sufficiently large number
- $C_S$  Maximum capacity of a shunting yard
- $C_M$  Maximum capacity of a marshaling yard





• Arc capacity constraints:

$$\sum_{k \in K} v^k \left( \sum_{i \in N} \sum_{j \in N} X_{ij}^k \left( b_{lm}^{k_0 i} + b_{lm}^{k_d j} + b_{lm}^{ij} \right) + (1 - z^k) b_{lm}^{k_0 k_d} \right) \le u_{lm}, \forall (l, m) \in A$$

Constants:

- $u_{lm}$  Capacity of the arc (l, m)
- $b_{lm}^{ij}$  Determines if arc (l, m) belongs to the shortest path between i and j





## Problem definition (cont.)

• Maximum number of yards:

$$\sum_{i \in N} s_i \le L_S \qquad \qquad \sum_{i \in N} m_i \le L_M$$

• Integrality constraints:

$$\begin{split} X_{ij}^k \in \{0,1\}, & \forall k \in K, \forall i \in N, \forall j \in N \\ & z^k \in \{0,1\}, & \forall k \in K \\ & r_i \in \{0,1\}, & \forall i \in N \\ & s_i \in \{0,1\}, & \forall i \in N \\ & m_i \in \{0,1\}, & \forall i \in N \end{split}$$





#### Problem size

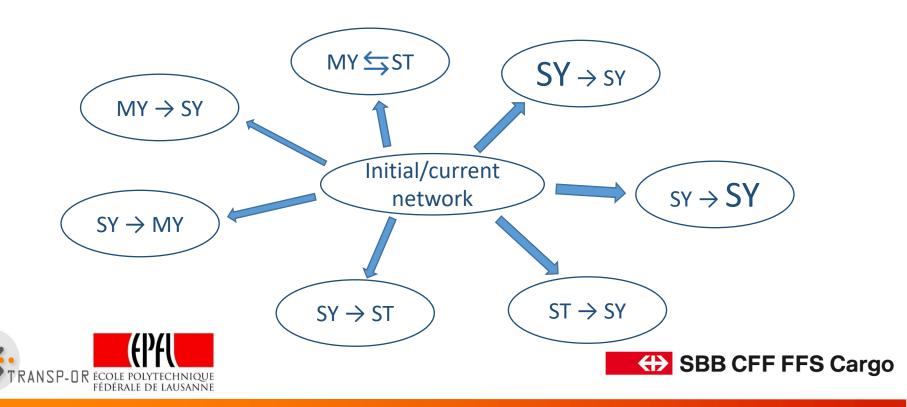
- Size of the SBB Cargo network:
  - Approx. 2100 stations
  - Approx. 2500 direct links
  - Over 65000 commodities





## Heuristic algorithm

- Hub location:
  - Adaptive large neighborhood search
  - Variable neighborhood search



## Heuristic algorithm - Neighborhoods



• Select the busiest station close to the MY and exchange their locations



• Select the least used MY and convert it into SY



• Select SY with fully utilized, maximum capacity and convert it into MY





## Heuristic algorithm - Neighborhoods



• Select SY with most unused capacity and decrease it



• Select SY with fully utilized, below-maximum capacity and increase it





## Heuristic algorithm - Neighborhoods



• Select underused SY with minimum capacity and convert it into a regular station



• Select frequently used regular station and convert it into a SY with minimum capacity





## Heuristic algorithm

- Commodity routing:
  - Prioritized assignment algorithm







## Heuristic algorithm - Path alternatives

- Direct (shortest) path
  - Unbundled commodity

- Via marshaling yards
  - Bundled commodity





## Heuristic algorithm - Path alternatives

- Via shunting yards
  - Bundled commodity
- Via one marshaling and one shunting yard
  - Bundled commodity





## Heuristic algorithm – development details

- Developed algorithm is very flexible:
  - Easily extendable with additional neighborhood operators, i.e. network transformations
  - Easy definition of specific initial network states, e.g. all marshaling yards closed, several additional marshaling yards open, etc.





## Preliminary results

- Network states with potential transportation cost reduction identified with two strategies (thus far):
  - I. SI:Allowing opening of new marshaling yards
  - 2. S2: Disallowing opening of new marshaling yards





## Preliminary results (cont.)

• Best resulting networks:

Strat.	New MY	Rem. MY	Mov. MY	Total MY	New SY	Rem. SY	Total SY	Cost reduct.
Orig. net.	-	-	-	2	-	-	50	-
<b>S1</b>	3	0	0	5	0	4	46	8.505%
S2	0	1	1	1	19	5	64	1.857%

- Daily transportation cost in the original network: over 38 Million CHF
- Running time: approx. 9h





## **Results discussion**

- Costs of transportation are dominant over yard operation costs
- Cost of yard maintenance is not taken into account
  - This cost contributes to reducing the number of yards and their size
  - Opening new yards will be less favored by the algorithm
  - Could be included in another case study
- New yards can be near the existing ones
  - E.g. in SI, new MY Territet is opened close to Lausanne MY
  - The objective function should penalize this situation





## Conclusions

- Developed algorithm explores various network changes, their combinations and their influence to the transportation costs
  - Flexible, easily extendable algorithm
- The algorithm identified network changes resulting in transportation cost reduction
- The objective function should be extended with the real **costs of maintenance** of the marshaling and shunting yards
  - Relevant change in the algorithm result





#### Future work

- Include penalty for having two yards near each other
- Solve the problem exactly on the subset of input data
  - To benchmark the heuristic result
- Implement visualization of the results
- Develop models based on MFP and MNDP
  - To compare results
  - If the current formulation cannot be solved exactly







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