

Vehicle Routing for a Complex Waste Collection Problem

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Overview

- 1 Introduction
- 2 Literature
- 3 Formulation
- 4 Solution Approach
- 5 Case Study
- 6 Conclusion
- 7 References

Overview

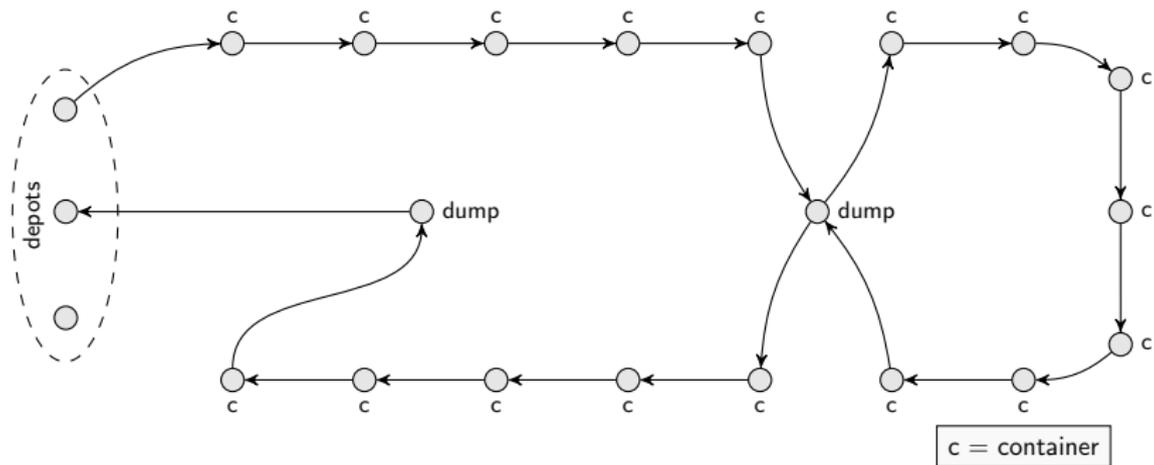
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 - volume capacities
 - weight capacities
 - fixed costs
 - unit distance running costs
 - hourly driver wage rates
 - speeds
 - site dependencies (accessibility constraints)

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- A set of containers placed at collection points with time windows
- A set of dumps (recycling plants) with time windows

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- A set of depots
- A set of containers placed at collection points with time windows
- A set of dumps (recycling plants) with time windows
- Maximum tour duration, interrupted by a break
- A tour is a sequence of collections and disposals at the available dumps, with a mandatory disposal before the tour end
- A tour need not finish at the depot it started from

Figure 1: Tour illustration



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- VRP with intermediate facilities:
 - VRP with satellite facilities (Bard et al., 1998)
 - no time windows, no driver break, homogeneous fleet
 - branch-and-cut
 - Waste collection VRP (Kim et al., 2006)
 - time windows, driver break, homogeneous fleet
 - simulated annealing
 - Ombuki-Berman et al. (2007) (GA), Benjamin (2011) (VNTS), Buhrkal et al. (2012) (ALNS) improve results by 15-16%
 - MDVRP with inter-depot routes (Crevier et al., 2007)
 - no time windows, no driver break, homogeneous fleet at single depot
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 - Tarantilis et al. (2008) (h-GLS), Hemmelmayr et al. (2013) (VNS) improve results by 1-3%
- Heterogeneous fixed fleet VRP:
 - Proposed by Taillard (1996)
 - Best exact solutions by Baldacci and Mingozzi (2009)
 - Best heuristic solutions by Subramanian et al. (2012) and Penna et al. (2013)

- Contribution:
 - Multiple depots
 - Multiple capacities
 - Realistic cost-based objective function
 - Simplification in the modeling of the dump visits
 - Non-time window constrained break
 - Incentive, rather than enforcement, to go back to the origin depot

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Sets and Parameters:

O' = set of origins

D = set of dumps

$N = O' \cup O'' \cup D \cup P$

K = set of vehicles

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ϕ_k = fixed cost of vehicle k

β_k = unit distance running cost of vehicle k

θ_k = hourly wage rate of vehicle k

Decision Variables:

$$x_{ijk} = \begin{cases} 1 & \text{if vehicle } k \text{ traverses edge } (i, j) \\ 0 & \text{otherwise} \end{cases}$$

$$b_{ijk} = \begin{cases} 1 & \text{if vehicle } k \text{ takes a break on edge } (i, j) \\ 0 & \text{otherwise} \end{cases}$$

$$y_k = \begin{cases} 1 & \text{if vehicle } k \text{ is used} \\ 0 & \text{otherwise} \end{cases}$$

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S_{ik} = start-of-service time of vehicle k at point i

Q_{ik}^V = cumulative volume on vehicle k at point i

Q_{ik}^W = cumulative weight on vehicle k at point i

$$\text{Min } f = \sum_{k \in K} \left(\phi_k y_k + \beta_k \sum_{i \in N} \sum_{j \in N} \pi_{ij} x_{ijk} + \theta_k \left(\sum_{j \in O''} S_{jk} - \sum_{i \in O'} S_{ik} \right) \right) \quad (1)$$

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$$x_{ijk} \leq \alpha_{ijk}, \quad \forall k \in K, i \in N \setminus O'', j \in N \setminus O' \quad (8)$$

$$\text{s.t. } Q_{ik}^v \leq \Omega_k^v, \quad \forall k \in K, i \in P \quad (9)$$

$$Q_{ik}^w \leq \Omega_k^w, \quad \forall k \in K, i \in P \quad (10)$$

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$$Q_{ik}^v + \rho_j^v \leq Q_{jk}^v + (1 - x_{ijk}) M, \quad \forall k \in K, i \in N \setminus O'', j \in P \quad (13)$$

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$$S_{ik} + \epsilon_i + \delta b_{ijk} + \tau_{ijk} \leq S_{jk} + (1 - x_{ijk}) M, \quad \forall k \in K, i \in N \setminus O'', j \in N \setminus O' \quad (15)$$

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$$\left(S_{ik} - \sum_{m \in O'} S_{mk} \right) + \epsilon_i - \eta \leq (1 - b_{ijk}) M, \quad \forall k \in K, i \in N \setminus O'', j \in N \setminus O' \quad (16)$$

$$\eta - \left(S_{jk} - \sum_{m \in O'} S_{mk} \right) \leq (1 - b_{ijk}) M, \quad \forall k \in K, i \in N \setminus O'', j \in N \setminus O' \quad (17)$$

$$b_{ijk} \leq x_{ijk}, \quad \forall k \in K, i, j \in N \quad (18)$$

$$\left(\sum_{j \in O''} S_{jk} - \sum_{i \in O'} S_{ik} \right) - \eta \leq \left(\sum_{\substack{i \in N \setminus O'' \\ j \in N \setminus O'}} b_{ijk} \right) M, \quad \forall k \in K \quad (19)$$

$$\text{s.t. } \lambda_i \sum_{j \in N \setminus O'} x_{ijk} \leq S_{ik} \leq \mu_i \sum_{j \in N \setminus O'} x_{ijk}, \quad \forall k \in K, i \in N \setminus O'' \quad (20)$$

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$$\text{s.t. } \lambda_i \sum_{j \in N \setminus O'} x_{ijk} \leq S_{ik} \leq \mu_i \sum_{j \in N \setminus O'} x_{ijk}, \quad \forall k \in K, i \in N \setminus O'' \quad (20)$$

$$\sum_{j \in O''} S_{jk} - \sum_{i \in O'} S_{ik} \leq H, \quad \forall k \in K \quad (21)$$

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$$\sum_{j \in O''} S_{jk} - \sum_{i \in O'} S_{ik} \leq H, \quad \forall k \in K \quad (21)$$

$$x_{ijk}, y_k, b_{ijk} \in \{0, 1\}, \quad \forall k \in K, i, j \in N \quad (22)$$

$$Q_{ik}^V, Q_{ik}^W, S_{ik} \geq 0, \quad \forall k \in K, i \in N \quad (23)$$

Extension:

$$z_{ijk} = \begin{cases} 1 & \text{if } i \text{ is the origin and } j \text{ the destination of vehicle } k \\ 0 & \text{otherwise} \end{cases}$$

Ψ = weight of relocation term

$$\text{Min } f = \text{Objective (1)} + \Psi \sum_{k \in K} \sum_{i \in O'} \sum_{j \in O''} (\beta_k \pi_{ji} + \theta_k \tau_{jik}) z_{ijk} \quad (24)$$

s.t. Constraints (2) to (23)

$$\sum_{m \in P} x_{imk} + \sum_{m \in D} x_{mjk} - 1 \leq z_{ijk}, \quad \forall k \in K, i \in O', j \in O'' \quad (25)$$

$$z_{ijk} = \{0, 1\}, \quad \forall k \in K, i \in O', j \in O'' \quad (26)$$

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- For small instances, common solver for the MILP formulation enhanced by valid inequalities and elimination rules, including:
 - Impossible traversals
 - Time window infeasible traversals
 - Latest start/earliest finish
 - Minimum tour duration
 - Symmetry breaking for subsets of identical vehicles
 - Minimum/maximum number of dump visits

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- For realistic-size instances, a feasibility preserving local search heuristic
- A feasible tour satisfies three criteria:
 - Time-window feasibility
 - Duration feasibility
 - Capacity feasibility
- The quality of the heuristic is assessed by benchmarking its results to the optimal ones obtained with the MILP model on small instances.

Figure 2: Temporal feasibility algorithm

Data: tour k as a sequence of points $1, \dots, n$ after a change

Result: start-of-service times, waiting times and temporal feasibility of tour k

set S_{1k} to earliest possible;

for $i = 2 \dots n$ in tour k **do**

 // Calculate tentative start-of-service times

$S_{ik} = S_{(i-1)k} + \epsilon_{i-1} + \tau_{(i-1)ik}$;

 // Insert break

if $S_{(i-1)k} + \epsilon_{i-1} \leq S_{1k} + \eta$ **and** $S_{ik} + \epsilon_i > S_{1k} + \eta$ **then**

 | $S_{ik} = S_{ik} + \delta$;

end

 // Calculate waiting times

if $S_{ik} < \lambda_i$ **then**

 | $w_{ik} = \lambda_i - S_{ik}$;

 | $S_{ik} = \lambda_i$;

else

 | $w_{ik} = 0$;

end

end

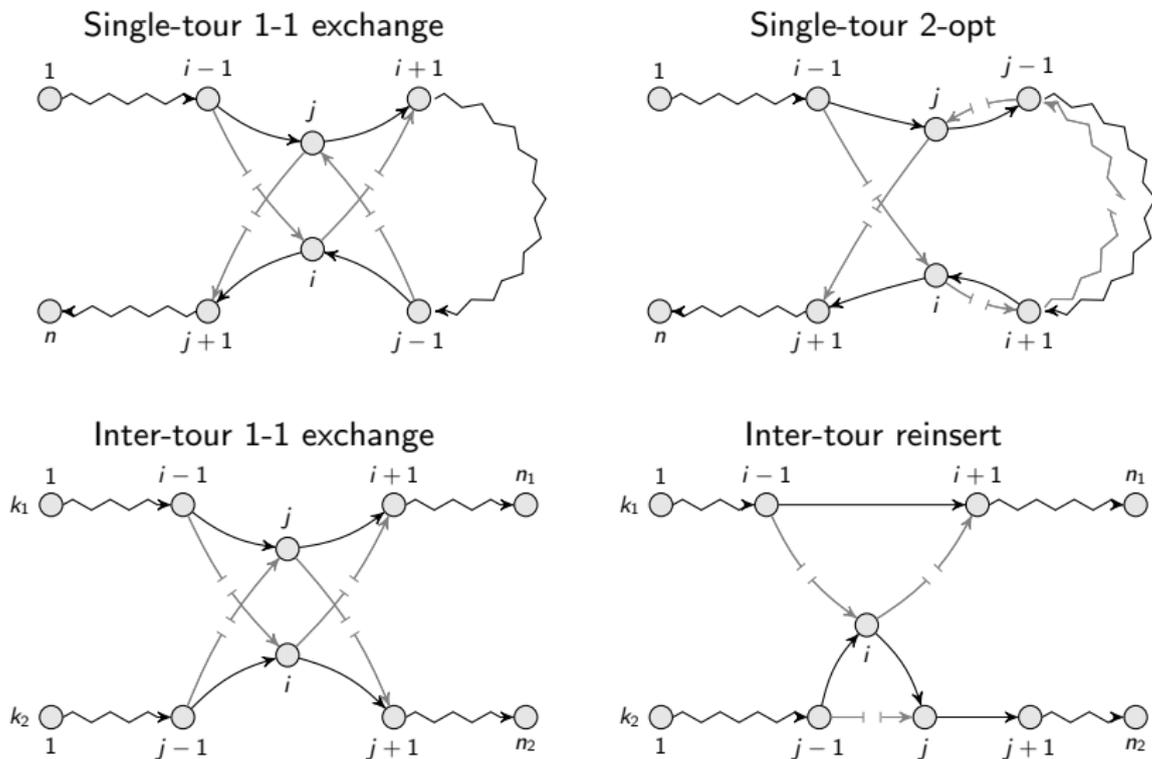
Figure 2: Temporal feasibility algorithm, cont'd

```

// Check time window feasibility
if  $S_{ik} \leq \mu_i, \forall i$  then
  // Forward time slack reduction
  for  $i = n \dots 2$  in tour  $k$  do
     $S'_{(i-1)k} = S_{(i-1)k}$ ;
     $S_{(i-1)k} = \min(S_{(i-1)k} + w_{ik}, \mu_{i-1})$ ;
     $w_{(i-1)k} = w_{(i-1)k} + (S_{(i-1)k} - S'_{(i-1)k})$ ;
     $w_{ik} = w_{ik} - (S_{(i-1)k} - S'_{(i-1)k})$ ;
  end
   $w_{1k} = 0$ ;
  // Check duration feasibility
  if  $S_{nk} - S_{1k} \leq H$  then
    | tour  $k$  is temporally feasible;
  else
    | discard tour  $k$  as duration infeasible;
  end
else
  | discard tour  $k$  as time-window infeasible;
end

```

Figure 3: Neighborhood operators



- Tour construction:
 - Sequential feasibility preserving insertion heuristic
 - At every iteration an unassigned container is inserted at the point that yields the smallest increase in the objective value
 - When container insertions would violate capacity, a dump is inserted using the same logic
 - A dump insertion should allow for at least one subsequent temporally feasible container insertion

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- Tour improvement:
 - Alternation between inter-tour and single-tour improvement
 - The application of an inter-tour operator is followed by single-tour improvement of the affected tours
 - Every operator is applied for *maxOplter* iterations and *maxOpNonImplter* non-improving iterations, before changing to the next operator
 - Both single-tour and multi-tour improvement run for *maxlter* iterations and *maxNonImplter* non-improving iterations
 - The resulting tour schedule is the best found during all iterations

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- 5 instances extracted randomly from real underlying data
- 3 versions of each instance:
 - No time windows (iX)
 - Wide time windows (iX_tw) - randomly assigned
 - Narrow time windows (iX_ntw) - randomly assigned
- 1 depot, 1 dump, 2 identical vehicles

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 - Narrow time windows (iX_ntw) - randomly assigned
- 1 depot, 1 dump, 2 identical vehicles
- Tests on 2.60 GHz Intel Core i7, 8GB of RAM
 - Local search heuristic coded in Java
 - Model solved on Gurobi 5.6.2 warm-started with the solutions from the local search heuristic
 - Solver time limit set to 1000 sec

Table 1: Comparison between heuristic and solver on random instances

$maxOplter = 100$, $maxOpNonImplter = 13$, $maxIter = 100$, $maxNonImplter = 1$

Instance	Heuristic		Solver				
	Objective	Runtime (sec.)	Objective	L Bound	MIP gap (%)	Runtime (sec.)	Opt gap (%)
i1	214.849	0.170	214.849	214.837	0.006	375.562	0.000
i1_tw	284.016	0.070	252.825	252.825	0.000	4.038	12.337
i1_ntw	428.539	1.093	394.817	394.817	0.000	0.922	8.541
i2	249.317	0.042	249.317	249.317	0.000	400.032	0.000
i2_tw	257.583	0.050	257.582	257.582	0.000	2.306	0.000
i2_ntw	460.635	0.756	439.769	439.769	0.000	2.420	4.745
i3	240.133	0.051	240.133	76.004	68.349	1000.000	0.000
i3_tw	245.457	0.070	245.457	245.457	0.000	2.894	0.000
i3_ntw	444.589	0.641	444.589	444.589	0.000	2.446	0.000
i4	138.643	0.077	138.643	138.643	0.000	521.509	0.000
i4_tw	140.204	0.030	140.204	140.204	0.000	7.660	0.000
i4_ntw	179.537	0.043	179.537	179.537	0.000	2.849	0.000
i5	220.770	0.070	220.770	129.834	41.190	1000.000	0.000
i5_tw	233.211	0.050	233.211	233.211	0.000	3.501	0.000
i5_ntw	405.622	0.848	405.622	405.622	0.000	3.051	0.000

Table 1: Comparison between heuristic and solver on random instances

$maxOplter = 100$, $maxOpNonImplter = 13$, $maxIter = 100$, $maxNonImplter = 1$

Instance	Heuristic		Solver				Opt gap (%)
	Objective	Runtime (sec.)	Objective	L Bound	MIP gap (%)	Runtime (sec.)	
i1	214.849	0.170	214.849	214.837	0.006	375.562	0.000
i1_tw	284.016	0.070	252.825	252.825	0.000	4.038	12.337
i1_ntw	428.539	1.093	394.817	394.817	0.000	0.922	8.541
i2	249.317	0.042	249.317	249.317	0.000	400.032	0.000
i2_tw	257.583	0.050	257.582	257.582	0.000	2.306	0.000
i2_ntw	460.635	0.756	439.769	439.769	0.000	2.420	4.745
i3	240.133	0.051	240.133	76.004	68.349	1000.000	0.000
i3_tw	245.457	0.070	245.457	245.457	0.000	2.894	0.000
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i5_ntw	405.622	0.848	405.622	405.622	0.000	3.051	0.000

Table 2: Comparison between heuristic and solver on selected random instances
maxOplter = 350, maxOpNonImplter = 37, maxIter = 100, maxNonImplter = 1

Instance	Heuristic		Solver				Opt gap (%)
	Objective	Runtime (sec.)	Objective	L Bound	MIP gap (%)	Runtime (sec.)	
i1_tw	252.825	0.410	252.825	252.825	0.000	3.487	0.000
i1_ntw	394.817	3.399	394.817	394.817	0.000	0.916	0.000
i2_ntw	439.769	3.080	439.769	439.769	0.000	2.309	0.000

Table 2: Comparison between heuristic and solver on selected random instances
maxOplter = 350, maxOpNonImplter = 37, maxIter = 100, maxNonImplter = 1

Instance	Heuristic		Solver				Opt gap (%)
	Objective	Runtime (sec.)	Objective	L Bound	MIP gap (%)	Runtime (sec.)	
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Overview

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- 2 Literature
- 3 Formulation
- 4 Solution Approach
- 5 Case Study
- 6 Conclusion**
- 7 References

- Conclusions:
 - Mathematical model
 - Local search heuristic
 - The heuristic performs favorably with an average optimality gap of less than 2% in short computation times (less than 1 sec)

- Conclusions:
 - Mathematical model
 - Local search heuristic
 - The heuristic performs favorably with an average optimality gap of less than 2% in short computation times (less than 1 sec)
- Future work
 - Mathematical model improvement to solve larger instances
 - Extension of the heuristic to include all features of the mathematical model
 - Development of efficient inter-tour operators to respond to the challenge posed by the heterogeneous fleet
 - Sensitivity analysis of the parameters
 - Benchmarking for realistic-size instances against current state of practice

Thank you for your attention!
Questions?

Overview

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