#### Bid-auction framework for microsimulation of location choice with endogenous real estate prices

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# Motivation

- Land use models
  - Travel demand forecast
  - Policy and project evaluation
- Location choice
  - Preferences of decision makers (willingness to pay)
  - Friction between agents (location conflicts) not always considered
- How are conflicts solved? → market
  - How to introduce this in a location choice model?



#### (residential) Real estate market

- Relatively scarce goods, almost inelastic demand
- Normally: A household can live in only one dwelling and a dwelling can't be used by more than one household
- Competition for goods implies conflict
- Conflict is solved through price adjustment
  - Changes in bid behavior of agents (bid-auction)
  - Changes in asking price of seller (choice)

interaction/transactions → market clearing (prices)





# **Motivation - Market clearing**

Modeling approaches to solve market clearing:

- Equilibrium (TRANUS, MEPLAN, MUSSA):
  - everyone is located or everything is sold
  - Aggregated
  - Cross sectional (no temporal dimension)
  - Fixed point problem
- Dynamic disequilibrium (DELTA, IRPUD, ILUTE, UrbanSim):
  - Aggregated or disaggregated (partial-eq. or individual transactions)
  - Period-wise models
  - Great variety of approaches (simplified vs expensive)





# **Market clearing**

Re-visiting equilibrium:

• For each good (location) *i* find asking prices  $r_i$  such that

$$\sum_{h} H_{h} P\left(i|h, r_{i}, P(i|\overline{h})\right) = S_{i} \quad \forall i$$

• For each household h, find bids  $B_{hi}$  such that

$$\sum_{i} S_{i} P\left(h|i, B_{hi}, P(\overline{h}|i)\right) = H_{h} \quad \forall h$$

Supply (households)

Demand (households)



## Idea

- Adjustment of price depends on the interaction between demand and supply → change in expected utility and bidding behavior given the "state of the market"
- Adjustment of expectation of agents before they enter the market can be based on the equilibrium approach to the problem.





# Proposal: Quasi-equilibrium approach

• Auction market. Probability of agent *h* being best bidder for location *i* (at period *t*):

$$P^{t}(h \mid i) = \frac{\exp(B_{hi}^{t})}{\sum_{g} \exp(B_{gi}^{t})}$$

• Price of location is the expected maximum bid

$$r_i^t = \ln\left(\sum_g \exp(B_{gi}^t)\right)$$





# Quasi-equilibrium approach

• Agents bid according to their preferences and their expected utility levels

$$B_{hi}^t = b_h^t + b_{hi}(z_i^t, \beta)$$

• Agents perceive their probability of winning an auction as:

$$q^{t}(h | i) = \frac{\exp(b_{h}^{t} + b_{hi}^{t})}{\sum_{g} \exp(B_{g}^{t})} \approx \exp(b_{h}^{t} + b_{hi}^{t} - r_{i}^{t-1})$$





# Quasi-equilibrium approach

• Agents will bid according to their perception of the market conditions: they want to make sure they get a location but they also don't want to over-bid

$$\sum_{i \in S^{t}} q^{t}(h|i) = \sum_{i \in S^{t}} \exp\left(b_{h}^{t} + b_{hi}(z_{i}^{t}, \beta) - r_{i}^{t-1}\right) = 1$$

$$b_h^t = -\ln\left(\sum_{i \in S^t} \exp\left(b_{hi}(z_i^t, \beta) - r_i^{t-1}\right)\right)$$





# Quasi-equilibrium approach

#### Market clearing mechanism:

- After adjusting their perceptions, all active households bid simultaneously for all locations available in the market in a period
- If a household is the best bidder for more than one location, the maximum surplus location is chosen (given  $r_i$ )
- Empty locations and unlocated households interact in a new simultaneous auctions
- Repeat until all households are located or all locations are occupied
- move to next period.





# Market clearing algorithm\*



# **General framework algorithm\***



## **Case study – Area of study**

 151 communes and 4945 zones around Brussels (approx 1.2 million households)







## **Case study – Data**

- Buildings: 4 types, average attributes at zone level (prices at commune level)
- Households: Data from Census (2001, zone level) and a travel survey (2002, ~1300 observations)
  - → Synthetic population

Attribute	levels		
Income level of the household $(inc_h)$	1 (0-1859 Euros)		
	2 (745-1859 Euros)		
	2 (1860-3099 Euros)		
	4 (3100-4958 Euros)		
	5 (>4959 Euros)		
Household size (hh_size <sub>h</sub> )	1,2,3,4,5+		
Number of children (children <sub>h</sub> )	0,1,2+		
Number of workers (workers <sub>h</sub> )	0,1,2+		
Number of cars (cars <sub>h</sub> )	0,1,2,3+		
Number of people with university degree (univ <sub>h</sub> )	0,1,2+		





Parameter	spatial attribute	×	household (hh) attribute	Parameter	Value	Std error	t-test
ASC <sub>2</sub>	-		income level 2 constant (745-1859 Euros)	ASC <sub>2</sub>	-0.171	0.083	-2.07
ASC <sub>3</sub>	-		income level 3 constant (1860-3099 Euros)	ASC <sub>3</sub>	-0.461	0.113	-4.1
ASC <sub>4</sub>	-		income level 4constant (3100-4958 Euros)	ASC <sub>4</sub>	2.05	0.374	5.47
ASC <sub>5</sub>	-		income level 5 constant (>4959 Euros)	ASC <sub>5</sub>	2.19	0.385	5.68
$\beta_{\text{house}}$	dummy for houses (types 1,2 or 3)	×	dummy for hh_size $_h > 2$ and inc $_h > 2$	$\beta_{ m house}$	-0.128	0.0472	-2.7
$\beta_{apartment}$	dummy for apartment (type 4)	×	dummy for hh_size $_h > 2$ and inc $_h > 2$	$\beta_{ m apartment}$	-0.702	0.181	-3.88
$\beta_{\text{surface}}$	surface of dwelling $v$ in zone $i$ (m <sup>2</sup> )	×	logarithm of hh_size <sub>h</sub>	$\beta_{\text{surface}}$	0.002	0.001	2.6
$\beta_{\text{high-inc}}$	% of hh's of income level 4 and 5 in commune $c$	×	dummy for income $inc_h > 2$	$\beta_{ m high-inc}$	3.97	1.24	3.21
$\beta_{\text{low-inc}}$	% of hh's of income level 1 and 2 in commune $\boldsymbol{c}$	×	dummy for income $inc_h > 3$	$\beta_{\text{low-inc}}$	-3.94	0.701	-5.62
$\beta_{\rm education}$	density of education jobs in commune c	×	dummy for $univ_h > 0$	$\beta_{ m education}$	0.356	0.127	2.8
$\beta_{\text{industry}}$	% of industry jobs in commune c	×	dummy for $inc_h > 3$	$\beta_{\text{industry}}$	-0.562	0.25	-2.25
$\beta_{\text{service}}$	% of service (office and hotel) jobs in zone <i>i</i>	×	dummy for workers $h > 0$	$\beta_{\text{service}}$	0.046	0.020	2.31
$\beta_{\rm shopping}$	density of retail jobs in zone <i>i</i>	×	dummy for income $inc_h > 2$	$eta_{ m shopping}$	0.040	0.018	2.24
$\beta_{\rm pubtrans}$	public transport acces <sub>i</sub> (facilities/km <sup>2</sup> )	×	dummy for $\operatorname{cars}_h = 0$	$\beta_{\rm pubtrans}$	0.257	0.094	2.72
$\beta_{\text{pubtrans2}}$	public transport acces <sub>i</sub> (facilities/km <sup>2</sup> )	×	dummy for $cars_h > 1$	$\beta_{\text{pubtrans2}}$	-0.249	0.101	-2.46
$\beta_{\text{car-access}}$	car accessibility in zone i (MATSim)	×	dummy for cars <sub>h</sub> > 0	$\beta_{\text{car-access}}$	0.007	0.004	1.9*
				α	-8.98	5.82	-1.54*

Hurtubia R. and Bierlaire M. (2012). Estimation of bid functions for location choice and price modeling with a latent variable approach. TRANSP-OR technical report.

NSP-OR



0.421

FÉDÉRALE DE LAUSANNE

3.46



γ

 $\sigma$ 

1.46

#### Observed and predicted population in 2008



ÉCOLE POLYTECHNIQUE FÉDÉRALE DE LAUSANNE



Variation in average income by commune 2001-2008













• Increase in price vs increase in income





Average real estate price by commune 2001 - 2008



Average real estate price by commune in 2008







# Conclusions

- Proposed approach accounts for adjustment of expectations of decision makers
- Individual adjustments allow to implement an agent based model (no need to solve fixed point problem)
- Results follow observed trends in spatial distribution of agents and evolution of prices
- Not considering market clearing produces an underestimation of prices





# Thank you





# Model with price indicator



# **Model with price indicator**

• Structural equation for prices:

$$r_i = \frac{1}{\mu} \ln \left( \sum_{g \in H} \exp(\mu B_{gi}) \right)$$

• Measurement equation for prices:

$$R_i = a + \gamma \cdot r_i$$

~ 
$$N(0,\sigma) \Rightarrow f(R_i | r_i) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{R_i - a - \gamma \cdot r_i}{2\sigma^2}\right)$$

Likelihood:

$$L = \prod_{i} \left( \prod_{h \in \mathcal{N}_{h/i}} \left( P_{h/i} \cdot f(R_i \mid r_i) \right)^{y_{hi}} \right)$$



