

TGF' 15

# A dynamic network loading model for anisotropic and congested pedestrian flows

Flurin S. Hänseler, William H.K. Lam, Michel Bierlaire,  
Gael Lederrey, Marija Nikolić

Delft, October 30, 2015

# Unsteady, anisotropic and congested flow

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**Figure:** Passageway in Central Station (MTR), Hong Kong

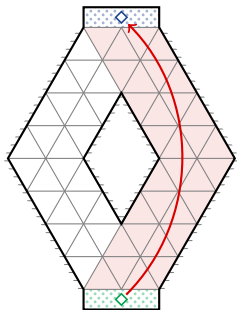
# Macroscopic pedestrian flow models

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- graph-based models [CS94, Løv94]
  - interaction between streams entirely neglected
- cell transmission models [ASKT07, GHW11, HBFM14]
  - inherent assumption of isotropy
- continuum models [Hug02, HWZ<sup>+</sup>09, HvWKDD14]
  - expensive, particularly for multi-class applications

# Time, space and demand

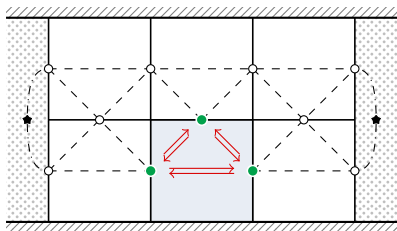
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- discrete time
  - uniform time intervals
- discrete space
  - partitioning into areas
- demand
  - pedestrian ‘groups’
  - aggregated by time interval and route
- route
  - origin/destination area
  - accessible network

# Walking network and model principle

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- **area:** range of interaction
- **stream:** uni-directional flow
- **node:** flow valve

- flow on uni-directional stream = density  $\times$  velocity
- stream-based pedestrian fundamental diagram (next slide)

# Pedestrian fundamental diagram

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- specification inspired by research at HKU [WLC<sup>+</sup>10, XW15]
- stream-based fundamental diagram (SbFD)

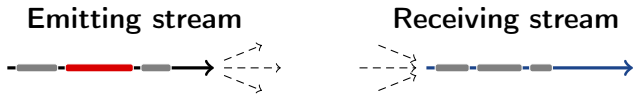
$$V_\lambda = V_f \cdot \exp\left\{-\vartheta k_\xi^2\right\} \prod_{\lambda' \in \Lambda_\xi} \exp\left(-\beta (1 - \cos \varphi_{\lambda, \lambda'}) k_{\lambda'}\right)$$

- isotropic reduction (Drake, 1967)
- reduction due to pair-wise interaction of streams

$V_f$ : free-flow speed,  $k_{\{\xi, \lambda\}}$ : density,  
 $\varphi_{\lambda, \lambda'}$ : intersection angle,  $\vartheta, \beta$ : parameters

# Propagation model

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① receiving capacity of **stream**

② sending capacity of **group fragment** to **stream**

③ candidate inflow to **stream**

④ actual flow of **group fragment** to **stream**

# Calibration

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- $\theta$ : unknown parameter vector
- pedestrian  $i = \{1, \dots, N\}$ 
  - $tt_i^{\text{obs}}$ : observed travel time
  - $f_i^{\text{est}}(tt|\theta)$ : estimated travel time probability density
- pseudo maximum likelihood estimation

$$\hat{\theta} = \arg \max \tilde{\mathcal{L}}(\mathbf{tt}_{\text{obs}}|\theta)$$

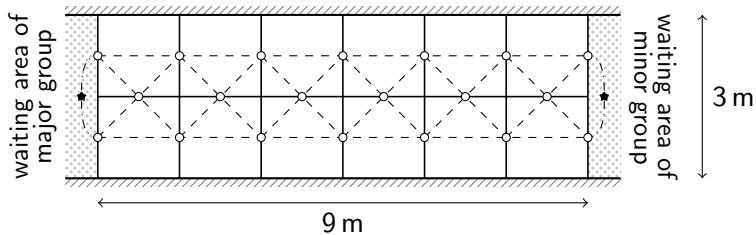
with

$$\tilde{\mathcal{L}}(\mathbf{tt}_{\text{obs}}|\theta) = \prod_{i=1}^N f_i^{\text{est}}(tt_i^{\text{obs}}|\theta)$$



# Counter-flow experiment (Wong et al., 2010)

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## Counter-flow experiment: Observed speeds

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Exp.	major group		minor group	
#84	87 ped	$1.08 \pm 0.15$ m/s	–	–
#85	79	$1.19 \pm 0.13$	9 ped	$0.80 \pm 0.14$ m/s
#86	68	$0.90 \pm 0.10$	18	$0.74 \pm 0.15$
#87	61	$0.82 \pm 0.06$	26	$0.67 \pm 0.10$
#88	53	$0.83 \pm 0.09$	30	$0.79 \pm 0.15$
#89	44	$0.79 \pm 0.10$	44	$0.79 \pm 0.18$

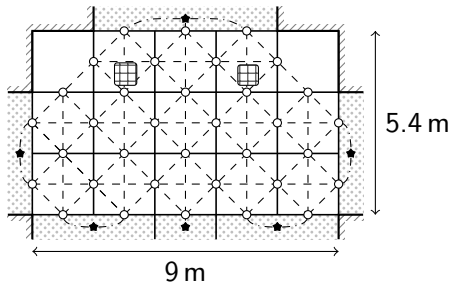
Extracted from Wong et al., 2010 [WLC<sup>+</sup>10]

# Counter-flow experiment: Results I

	Zero-Model	Drake	SbFD	Weidmann
$AIC_{85,87}^{\text{calib}}$	837.7	754.0	704.5	729.4
$v_f$ [m/s]	$1.166 \pm 0.001$	$1.170 \pm 0.001$	$1.115 \pm 0.000$	$1.169 \pm 0.001$
$\mu$ [-]	$1.43 \pm 0.06$	$12.15 \pm 0.29$	$10.18 \pm 2.02$	$14.84 \pm 0.30$
$\vartheta$ [m <sup>4</sup> ]		$0.078 \pm 0.000$	$0.001 \pm 0.004$	
$\beta$ [m <sup>2</sup> ]			$0.210 \pm 0.005$	
$\gamma$ [m <sup>-2</sup> ]				$4.92 \pm 0.20$
$k_j$ [m <sup>-2</sup> ]				$6.58 \pm 0.46$
$AIC_{84}^{\text{valid}}$	355.2	338.4	311.4	348.2
$AIC_{86}^{\text{valid}}$	381.7	371.3	355.3	401.4
$AIC_{88}^{\text{valid}}$	400.3	384.6	364.0	435.3
$AIC_{89}^{\text{valid}}$	458.2	408.8	396.8	454.6

# Cross-flow experiment (Plaue et al., 2014)

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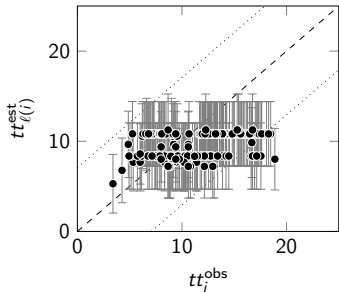
# Cross-flow experiment: Results I

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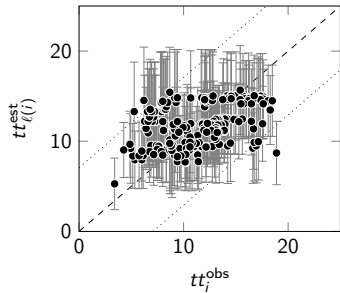
**Table:** Results of calibration on cross-flow experiment.

	Zero-Model	Drake	SbFD	Weidmann
AIC	1160.0	1101.0	1062.6	1098.8
$v_f$ [m/s]	$1.307 \pm 0.005$	$1.308 \pm 0.001$	$1.308 \pm 0.006$	$1.332 \pm 0.002$
$\mu$ [-]	$1.16 \pm 0.03$	$1.39 \pm 0.02$	$2.64 \pm 0.41$	$2.05 \pm 0.20$
$\vartheta$ [m <sup>4</sup> ]		$0.139 \pm 0.004$	$0.143 \pm 0.004$	
$\beta$ [m <sup>2</sup> ]			$0.300 \pm 0.008$	
$\gamma$ [m <sup>-2</sup> ]				$1.76 \pm 0.15$
$k_j$ [m <sup>-2</sup> ]				$5.99 \pm 0.61$

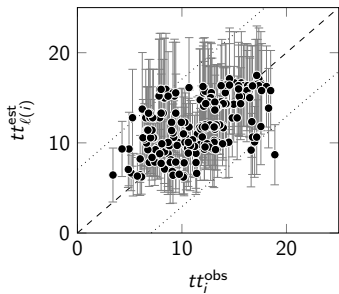
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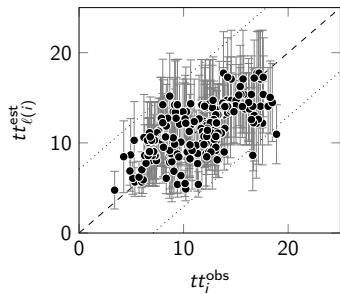
(a) Zero-Model ( $L^2$ -error: 53.3 s)



(b) Drake ( $L^2$ -error: 47.6 s)

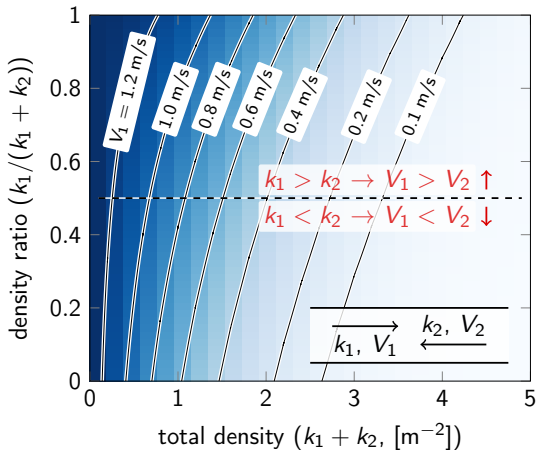


(c) Weidmann ( $L^2$ -error: 47.4 s)



(d) SbFD ( $L^2$ -error: 39.2 s)

# Illustration: Walking speed in counter-flow



Parameters:

$$V_f = 1.308 \text{ m/s}$$

$$\vartheta = 0.143 \text{ m}^4$$

$$\beta = 0.300 \text{ m}^2$$

(Berlin data set)

## Concluding remarks

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- macroscopic model for congested, anisotropic flow
  - stream-based pedestrian fundamental diagram
  - freely available on GitHub
- counter- and cross-flow experiments
  - significant improvement for anisotropic formulation
- future work
  - applications within DTA-framework, demand estimation



# Thank you

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TGF' 15:

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## Counter-flow experiment: Results II

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**Table:** Travel times for counter-flow validation experiments.

Exp.	Groups	$tt_{\text{obs}}$ [s]	$tt_{\text{Zero}}$ [s]	$tt_{\text{Drake}}$ [s]	$tt_{\text{SbFD}}$ [s]	$tt_{\text{Weidmann}}$ [s]
#84	87 / 0	8.5 / -	9.5 / -	9.1 / -	8.1 / -	8.3 / -
#86	68 / 18	10.1 / 12.7	9.5 / 9.5	10.0 / 10.8	9.4 / 12.5	8.8 / 9.5
#88	53 / 31	10.9 / 11.8	9.5 / 9.5	10.0 / 10.6	10.3 / 11.7	8.9 / 9.2
#89	44 / 44	11.8 / 11.6	9.5 / 9.5	11.6 / 11.4	11.7 / 11.6	9.7 / 9.9
L <sup>2</sup> -error (weighted, [s])			21.4 / 23.4	9.0 / 10.5	7.9 / 0.7	22.3 / 23.3

## Cross-flow experiment: Results II

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**Table:** Travel times along major routes in Berlin case study.

$N_{\text{ped}}$	$tt_{\text{obs}}$ [s]	$tt_{\text{Zero}}$ [s]	$tt_{\text{Weidmann}}$ [s]	$tt_{\text{Drake}}$ [s]	$tt_{\text{SbFD}}$ [s]
118	12.4 (base)	10.8 (-12.7%)	14.0 (+12.6%)	13.3 (+7.2%)	12.6 (+1.8%)
46	10.6 (base)	8.4 (-21.3%)	9.9 (-6.8%)	10.0 (-6.2%)	10.9 (+2.2%)