



Workshop in Discrete Choice Models

# **Activity path size for correlation between activity paths**

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# Outline

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Motivation: Activity-based model for pedestrian facilities

A path choice approach to activity modeling

Correlation between activity paths

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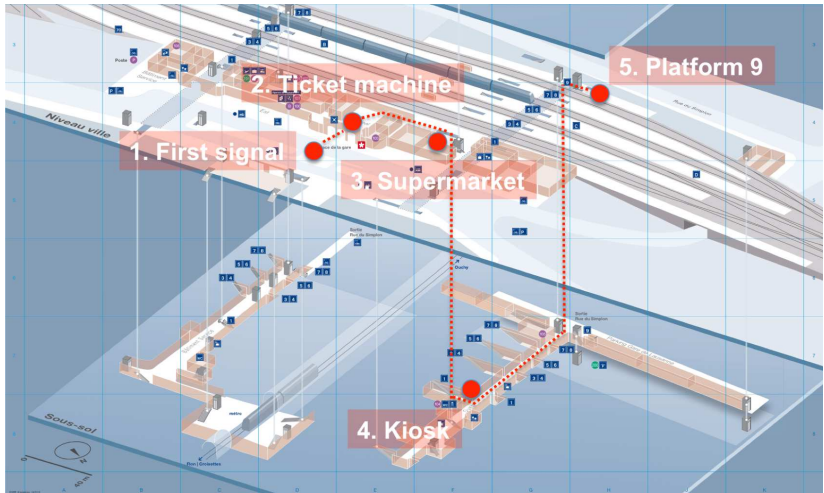
Correlation between activity paths

# Activities in pedestrian infrastructure

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# Spatial choices in pedestrian infrastructure



# Motivation

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- **Activity-based approach:** modeling the activity participation patterns
- **Not tour-based** (no “home” location in pedestrian facilities)
- **No hierarchy** of dimensions or aggregation

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# Notation

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- Measurement  $\hat{m} = (\hat{x}, \hat{t})$  (e.g., WiFi traces)

$$(\hat{m}_1, \hat{m}_2, \dots, \hat{m}_J) = \hat{m}_{1:J}$$

- Activity episode  $a = (x, t^-, t^+)$  (e.g., BC, 12:10-14:10)

$$(a_1, a_2, \dots, a_\Psi) = a_{1:\Psi}$$

- Activity type  $\mathcal{A}_k$  (e.g., eating)
- Activity  $A = (\mathcal{A}_k, t^-, t^+)$  (e.g., eating, 12:10-14:10)

$$(A_1, A_2, \dots, A_\Psi) = A_{1:\Psi}$$



# Goal

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Model the activity-episode sequence  $a_{1:\psi}$   
when observing  $\hat{m}_{1:J}$  from antennas

Raw data

**Pre-processing**

Activity-episode sequence detection [DFB14]

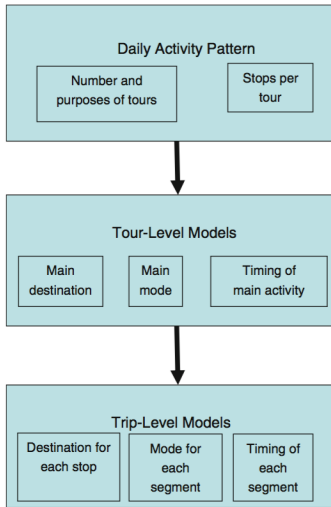
**Modeling**

Activity path choice model [DB15]

Destination choice model [TDdLB15]

# Yoram's model

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# Path choice approach to activity modeling

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## 1. Input

- 1.1 Network traces  $\hat{m}_{1:J}$
- 1.2 Semantically-enriched routing graph
- 1.3 Potential attractivity measure

## 2. Pre-processing

- 2.1 Activity-episode sequence  $a_{1:\psi}$  detection [DFB14]

$$P(a_{1:\psi} | \hat{m}_{1:J}) \propto P(\hat{m}_{1:J} | a_{1:K}) \cdot P(a_{1:\psi})$$

## 3. Modeling

- 3.1 Activity path choice model [DB15]
- 3.2 Destination choice model [TDdLB15]

# Modeling assumption

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- Sequential choice:

1. activity type, sequence, time of day and duration

$$P(A_{1:\psi})$$

2. destination choice conditional on 1.

$$P(x|A_{1:\psi})$$

- Motivations:

- Behavior: precedence of activity choice over destination choice
- Dimensional: destinations  $\times$  time  $\times$  order is large

Today, we focus on 1. [DB15].

# Full model

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Probability of reproducing observations  $\hat{m}_{1:J}$  of individual  $i$  is

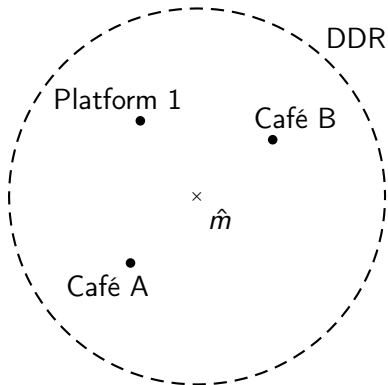
$$P_i(\hat{m}_{1:J}) = \sum_{a_{1:\psi} \in \mathcal{C}} P(\hat{m}_{1:J} | a_{1:\psi}) \cdot P(a_{1:\psi}) \quad (1)$$

$$= \sum_{a_{1:\psi} \in \mathcal{C}} P(\hat{x}_{1:J} | x_{1:\psi}) \cdot P(A_{1:\psi}) \cdot P(x | A_{1:\psi}) \quad (2)$$

$$= \sum_{a_{1:\psi} \in \mathcal{C}} \prod_{j=1}^J P(\hat{x}_j^\psi | x_\psi) \cdot P(A_{1:\psi}) \cdot \prod_{\psi=1}^\Psi P(x | A_\psi) \quad (3)$$

## Toy example

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$$P(\hat{m}) = \frac{2}{3}P(\text{Café}) \cdot \left( P(\text{Café A}|\text{Café}) + P(\text{Café B}|\text{Café}) \right) + \frac{1}{3}P(\text{Platform}) \cdot P(\text{Platform 1}|\text{Platform})$$

# Observations: activity patterns in a transport hub

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## Activity types

Waiting for the train

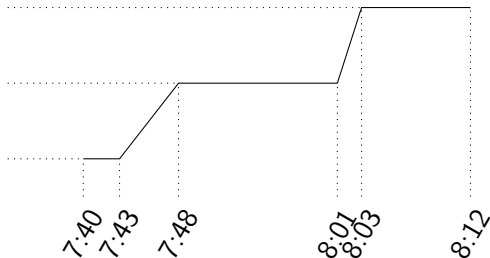
(on platform 1)

Having a coffee

(in Café A)

Buying a ticket

(at the machine)



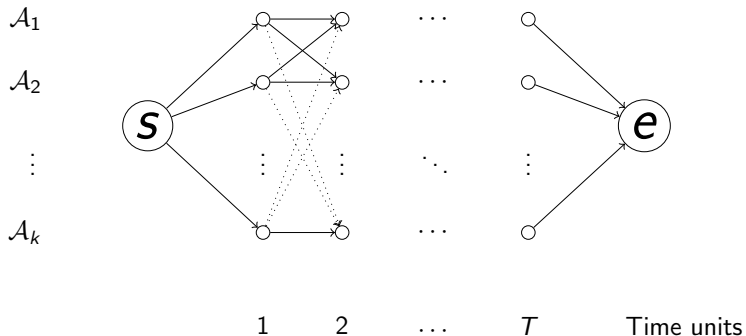


# Activity path

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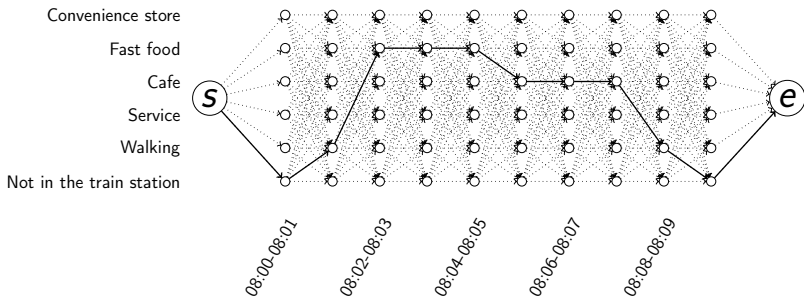
Activity types

Activity network



# Activity network

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# Challenge 1: Choice set generation

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- Simple random sampling: observations dominate alternatives
- Importance sampling  
using Metropolis-hastings algorithm [FB13]
  - Observation score [Che13]
  - Strategic sampling [LK12]

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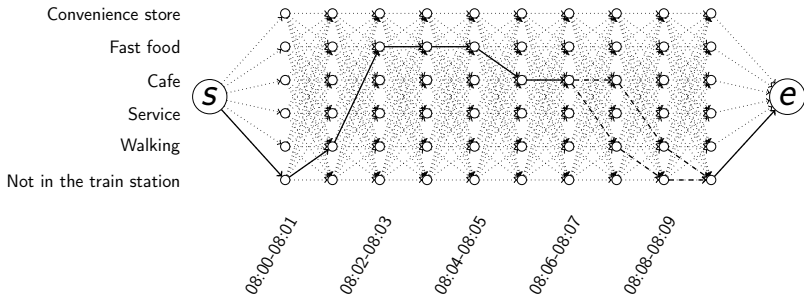
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## Challenge 2: Correlation between activity paths

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- IIA property might not hold
- Activity paths share unobserved attributes
- Due to overlaps?
- Deterministic correction: Activity Path Size?

# Route path size

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- Aggregation of alternatives [BAL85]
  - Elemental alternatives: activity paths
  - Aggregate alternatives: nodes in the activity network
- Size of aggregate alternative: number of paths using this link
- In activity network: constant,  $K^{\tau-1}$ , cancels out, no correction.

# Activity Path Size

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- Similarity measure: shared primary activity [Bow98]
  - Primary activity  $\mathcal{A}_p$ : relative majority of nodes
  - Size of node: nb of paths using it, with primary activity  $\mathcal{A}_p$
- Similarity measure: shared pattern
  - Pattern  $p$ : ordered sequence of activity types, without duration
    - ▶ Activity path: Home-Home-Home-Work-Work-Work-Work-Work-Shop-Home-Home
    - ▶ Activity pattern: Home-Work-Shop-Home
  - Size of node: number of paths using the node, with pattern  $p$

## Primary Activity Path Size

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- Node  $\mathcal{A}_{k,\tau}$  corresponds to primary activity  $\mathcal{A}_p$

$$M_{\mathcal{A}_{k,\tau}} = \left[ \frac{x^{T-1}}{(T-1)!} \right] \sum_{j \geq 0} \frac{x^{j-1}}{(j-1)!} \left( 1 + x + \frac{x^2}{2!} + \cdots + \frac{x^{j-1}}{(j-1)!} \right)^{K-1}$$

- Node  $\mathcal{A}_{k,\tau}$  does not correspond to primary activity  $\mathcal{A}_p$

$$M_{\mathcal{A}_{k,\tau}} = \left[ \frac{x^{T-1}}{(T-1)!} \right] \sum_{j \geq 0} \frac{x^j}{j!} \left( 1 + x + \frac{x^2}{2!} + \cdots + \frac{x^{j-1}}{(j-1)!} \right)^{K-2} \left( 1 + x + \frac{x^2}{2!} + \cdots + \frac{x^{j-2}}{(j-2)!} \right)$$



## Activity Pattern Path Size

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$$M_{A_k, \tau} = \sum_{i=1}^{|p_k|} \binom{\tau - 1}{L_i - 1} \binom{T - \tau}{|p| - L_i}$$

- $|p|$ : number of elements in pattern  $p$
- $|p_k|$ : number of times activity type  $k$  appears in pattern  $p$
- $L_i$ : index of the  $i$ th occurrence of activity type  $k$  in pattern  $p$

# Conclusion

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- Network traces can be used for estimation of activity-based models in pedestrian facilities
- Activity path approach models pattern, time of day, duration and number of episodes simultaneously, using recent developments in route choice modeling
- Similar paths are probably correlated; deterministic correction proposed

## Future work

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- Estimate a model with Primary Activity Path Size and Activity Pattern Path Size
- Cross nested logit model with sampling of alternatives for route choice models [LB14] adapted to activity path choice

# Thank you

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Workshop in Discrete Choice Models:

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