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# Behavioural Pedestrian Tracking (II)

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# Outline

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- Visual tracking
- Pedestrian Visual Tracking
- Evolution of the approach
- Future work

# Visual Tracking

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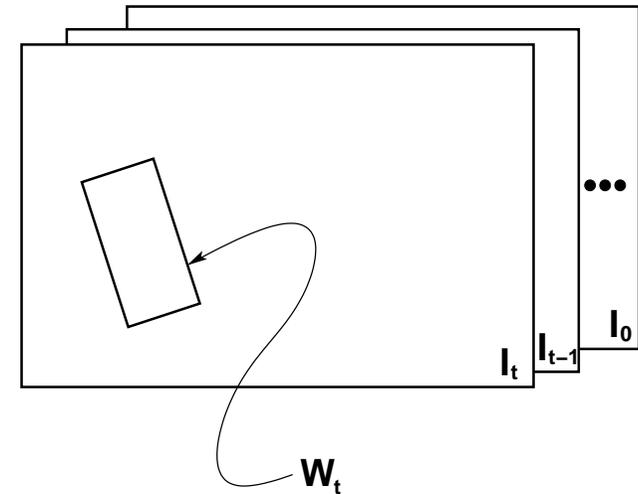
Ross, D., Lim, J. and Lin, R.-S. (2008), *Incremental Learning for Robust Visual Tracking*. International Journal of Computer Vision 77: 125-141.

- On-Line low-dimensional subspace representation (incremental PCA)
- Gaussian variables
- (Particle filtering)

# Visual Tracking

## Definitions:

- $I_t$ : frame  $t$
- $X_t = (x_t, y_t)$ : position
- $\varphi_t$ : rotation
- $\gamma_t$ : skewness
- $s_t$ : scale
- $r_t = \frac{w_t}{h_t}$ : aspect ratio
- $W_t = f(I_t, X_t, \varphi_t, \gamma_t, s_t, r_t)$ : a patch in  $I_t$
- $\Psi_t = \{X_t, \theta_t\} = \{X_t, \varphi_t, \gamma_t, s_t, r_t\} \in \Theta_t$



# Visual Tracking

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Everything is supposed to be Gaussian:

- $X_t \sim \mathcal{N}(X_{t-1}, \sigma_X)$
- $\varphi_t \sim \mathcal{N}(\varphi_{t-1}, \sigma_\varphi)$
- $\gamma_t \sim \mathcal{N}(\gamma_{t-1}, \sigma_\gamma)$
- $s_t \sim \mathcal{N}(s_{t-1}, \sigma_s)$
- $r_t \sim \mathcal{N}(r_{t-1}, \sigma_r)$

$$\Psi_t = \{X_t, \varphi_t, \gamma_t, s_t, r_t\} \in \Theta_t$$

# Visual Tracking

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$$\Psi_t^* = \arg \max_{\Psi_t \in \Theta_t} p(I_t | \Psi_t) p(\Psi_t | \Psi_{t-1})$$

Observation:

$$p(I_t | \Psi_t) \sim \mathcal{N}(W_t; \mu, UU^\top + \varepsilon I) \mathcal{N}(W_t; \mu, U \Sigma_o^{-2} U^\top)$$

Dynamics:

$$p(\Psi_t | \Psi_{t-1}) \sim \mathcal{N}(\Psi_t; \Psi_{t-1}, \Sigma_\Psi)$$

# Visual Tracking

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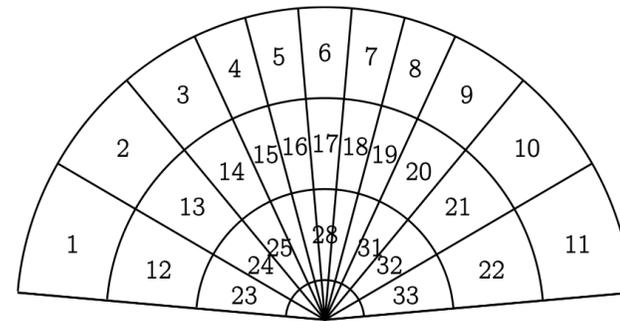
(Visual Tracking demo)

# Behavioural Visual Tracking

Robin, T., Antonini, G., Bierlaire, M., and Cruz, J. (2009), *Specification, estimation and validation of a pedestrian walking behavior model*.  
Transportation Research Part B: Methodological 43(1):36-56.

Next step given by a cross-nested logit model that takes into account:

- Direction
- Destination
- Speed
- “Leader-follower”
- “Collision avoidance”



Choice Set

# Behavioural Visual Tracking

$$\begin{aligned}
 & V_{v_{dn}} = \beta_{\text{dir\_central}} \text{dir}_{dn} I_{d,\text{central}} & + & \\
 & \beta_{\text{dir\_side}} \text{dir}_{dn} I_{d,\text{side}} & + & \\
 & \beta_{\text{dir\_extreme}} \text{dir}_{dn} I_{d,\text{extreme}} & + & \left. \vphantom{\beta_{\text{dir\_central}}} \right\} \textit{keep direction} \\
 & \beta_{\text{ddist}} \text{ddist}_{v_{dn}} & + & \\
 & \beta_{\text{ddir}} \text{ddir}_{dn} & + & \left. \vphantom{\beta_{\text{ddist}}} \right\} \textit{toward destination} \\
 & \beta_{\text{dec}} I_{v,\text{dec}} (v_n / v_{\text{max}})^{\lambda_{\text{dec}}} & + & \\
 & \beta_{\text{accLS}} I_{n,\text{LS}} I_{v,\text{acc}} (v_n / v_{\text{maxLS}})^{\lambda_{\text{accLS}}} & + & \left. \vphantom{\beta_{\text{dec}}} \right\} \textit{free flow acceleration} \\
 & \beta_{\text{accHS}} I_{n,\text{HS}} I_{v,\text{acc}} (v_n / v_{\text{max}})^{\lambda_{\text{accHS}}} & + & \\
 & I_{v,\text{acc}} I_{d,\text{acc}}^L \alpha_{\text{acc}}^L D_L^{\rho_{\text{acc}}^L} \Delta v_L^{\gamma_{\text{acc}}^L} \Delta \theta_L^{\delta_{\text{acc}}^L} & + & \\
 & I_{v,\text{dec}} I_{d,\text{dec}}^L \alpha_{\text{dec}}^L D_L^{\rho_{\text{dec}}^L} \Delta v_L^{\gamma_{\text{dec}}^L} \Delta \theta_L^{\delta_{\text{dec}}^L} & + & \left. \vphantom{I_{v,\text{acc}}} \right\} \textit{leader-follower} \\
 & I_{d,d_n} I_{d,C} \alpha_C e^{\rho_C D_C} \Delta v_C^{\gamma_C} \Delta \theta_C^{\delta_C} & & \left. \vphantom{I_{d,d_n}} \right\} \textit{collision avoidance}
 \end{aligned}$$

# Behavioural Visual Tracking

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This forces some assumptions:

- Camera is calibrated
- Camera is fixed
- Pedestrians walking in normal conditions
- Destination known!!

# Behavioural Visual Tracking

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Pedestrian model + Gaussian:

- $X_t \sim$  pedestrian walking behaviour model (PWBM)
- $\varphi_t \sim \mathcal{N}(\varphi_{t-1}, \sigma_\varphi)$
- $\gamma_t \sim \mathcal{N}(\gamma_{t-1}, \sigma_\gamma)$
- $s_t \sim \mathcal{N}(s_{t-1}, \sigma_s)$
- $r_t \sim \mathcal{N}(r_{t-1}, \sigma_r)$

$$\Psi_t = \{X_t, \theta_t\} = \{X_t, \varphi_t, s_t, r_t\} \in \Theta_t$$

Note that as calibration data is known, some corrections can be done in the sizes of the windows

# Behavioural Visual Tracking

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$$\Psi_t^* = \arg \max_{\Psi_t \in \Theta_t} p(I_t | \Psi_t) p(\Psi_t | \Psi_{t-1})$$

Observation:

$$p(I_t | \Psi_t) \sim \mathcal{N}(W_t; \mu, UU^\top + \varepsilon I) \mathcal{N}(W_t; \mu, U \Sigma_o^{-2} U^\top)$$

Dynamics:

$$p(\Psi_t | \Psi_{t-1}) \sim \text{PWBM}(X_t; X_{t-1}) \mathcal{N}(\theta_t; \theta_{t-1}, \Sigma_\theta)$$

# Behavioural Visual Tracking

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(Behavioural Visual Tracking demo)

# One step further (literally)

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The idea in order to solve the problems of the current approach is to delay the decision, i.e. propagate probability distributions during several frames instead of choosing the winner for each frame.

Advantages:

- Occlusions
- Trajectory “coherence”

Drawbacks:

- Interdependence (collision avoidance and leader follower)

# One step further (literally)

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Simulation-based tracking:

trajectory simulation + probability distribution of patches

Signal processing on manifolds:

- Probability distribution of patches
- Define a measure

One problem: 0.5 seconds!

# Future work

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- Develop formally these ideas (define the manifold and the measure)
- Implement and test
- Instead of a window, define something more similar to a pedestrian in 3D