

Enseignant: M. Bierlaire  
 Assistante: Sh. Sharif Azadeh

---

**Optimisation linéaire : Dualité**


---

**Question 1:**

(à résoudre sur le tableau par le chargé de cours)

- a) Formulate the dual problem of the following linear program without converting it into canonical form.

$$\begin{aligned}
 \min \quad & -x_1 - x_2 \\
 & x_1 - 2x_2 = 0 \\
 & x_1 + x_2 \leq 7 \\
 & 2x_1 + x_2 \geq 2 \\
 & x_1 \in \mathbb{R} \\
 & x_2 \geq 0
 \end{aligned}$$

- b) Complete the following table by indicating whether different combinations between a primal and dual program are possible or not.

Dual/Primal	Optimal	Unbounded	Infeasible
Optimal			
Unbounded			
Infeasible			

**Question 2:**

(à résoudre par les étudiants en classe)

Write the dual of the following problems without converting it into the standard or canonical form.

- a)

$$\begin{aligned}
 \min \quad & x_1 - 4x_2 + 2x_3 \\
 & 2x_1 + x_2 \geq 10 \\
 & x_1 + 4x_3 = 16 \\
 & x_2 - x_3 \leq 5 \\
 & x_1 \geq 0 \\
 & x_2 \in \mathbb{R} \\
 & x_3 \leq 0
 \end{aligned}$$



Enseignant: M. Bierlaire  
Assistante: Sh. Sharif Azadeh

Introduction  
à l'optimisation  
Fall 2014 - 2015

---

**Optimisation linéaire : Dualité**

---

b)

$$\begin{aligned} \min & -4x_1 - 7x_2 \\ & -5x_1 + 4x_2 \leq 16 \\ & x_1 + 3x_2 \leq 31 \\ & x_1 + 2x_2 \leq 24 \\ & 3x_1 + 5x_2 \leq 68 \\ & x_1 + x_2 \leq 22 \\ & X \geq 0 \end{aligned}$$

**Question 3:**

(à résoudre par les étudiants en classe)

**Demonstration:** Show when the dual of a given optimization problem is similar to its primal. Give an example.