
Introduction to choice models

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Modeling behavior

- Individual behavior (vs. aggregate behavior)
- Theory of behavior which is:
 - **descriptive**: how people behave and not how they should;
 - **abstract**: not too specific;
 - **operational**: can be used in practice for forecasting.
- Type of behavior: **choice**

Motivations

Field :

- ▶ Marketing
- ▶ Transportation
- ▶ Politics
- ▶ Management
- ▶ New technologies

Type of behavior:

- ▶ Choice of a brand
- ▶ Choice of a transportation mode
- ▶ Choice of a president
- ▶ Choice of a management policy
- ▶ Choice of investments

Importance

Daniel
L.
McFadden



1937–

- UC Berkeley 1963, MIT 1977, UC Berkeley 1991;
- Laureate of *The Bank of Sweden Prize in Economic Sciences in Memory of Alfred Nobel 2000*;
- Owns a farm and vineyard in Napa Valley;
- “Farm work clears the mind, and the vineyard is a great place to prove theorems”.

Example

Travel Information System:

- What is the market penetration?
- How will the penetration change in the future?
- Assumption: level of education is an important explanatory factor.

Data collection:

- Sample of 600 persons, randomly selected;
- Two questions:
 1. Do you subscribe to a travel information system? (yes/ no)
 2. How many years of education have you had? (low/ medium/ high)

Example (cont.)

- Contingency table

TIS	Education			
	Low	Medium	High	
Yes	10	100	120	230
No	140	200	30	370
	150	300	150	600

- Penetration in the sample: $230/600 = 38.3\%$
- Forecasting: need for a model

Example: A model

- Dependent variable:

$$y = \begin{cases} 1 & \text{if subscriber} \\ 2 & \text{if not subscriber} \end{cases}$$

Discrete dependent variable

- Independent or explanatory variable

$$x = \begin{cases} 1 & \text{if level of education is low} \\ 2 & \text{if level of education is medium} \\ 3 & \text{if level of education is high} \end{cases}$$

Example: A model (cont.)

- Market penetration in the sample: $\hat{p}(y = 1)$
- Market penetration in the population: $p(y = 1)$ estimated by $\hat{p}(y = 1)$
- Joint probabilities: $\hat{p}(y = 1, x = 2) = 100/600 = 0.1667$
- Marginal probabilities:
$$\hat{p}(y = 1) = \sum_{k=1}^3 \hat{p}(1, k) = 10/600 + 100/600 + 120/600 = 0.383$$
- Conditional probabilities: $\hat{p}(y = 1|x = 2)$

$$\begin{aligned}\hat{p}(y = 1, x = 2) &= \hat{p}(y = 1|x = 2)\hat{p}(x = 2) \\ \hat{p}(y = 1|x = 2) &= \hat{p}(y = 1, x = 2)/\hat{p}(x = 2) \\ &= 0.1667/0.5 = 0.333\end{aligned}$$

Example: A model (cont.)

Similarly, we obtain:

$$\hat{p}(y = 1|x = 1) = 0.067$$

$$\hat{p}(y = 1|x = 2) = 0.333$$

$$\hat{p}(y = 1|x = 3) = 0.8$$

We obtain a causal relationship.

- Behavioral model: $\hat{p}(y = i|x = j)$
- Forecasting assumption: stable over time

Example: Forecasting

- Model:

$$p(y = 1|x = 1) = \pi_1 = 0.067$$

$$p(y = 1|x = 2) = \pi_2 = 0.333$$

$$p(y = 1|x = 3) = \pi_3 = 0.8$$

where π_1, π_2, π_3 are estimated parameters.

- Assumption: future level of education: 10%-60%-30%

$$\begin{aligned} p(y = 1) &= \sum_{i=1}^3 p(y = 1|x = i)p(x = i) \\ &= 0.1\pi_1 + 0.6\pi_2 + 0.3\pi_3 \\ &= 44.67\% \end{aligned}$$

Example: Forecasting (cont.)

- If the level of education increases
- from 25%-50%-25% to 10%-60%-30%,
- the market penetration of TIS will increase
- from 38.33 % to 44.67%.

In summary:

- $p(x = j)$ can be easily obtained and forecasted;
- $p(y = i|x)$ is the behavioral model to be developed.

Bibliography

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