

Decision-Aid Methodologies in Transportation

Optimization Exercise 1

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1 Software

- IBM ILOG CPLEX Optimization Studio
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IBM ILOG CPLEX Optimization Studio

Shopping cart items

| Quantity | Part number | IBM price excluding tax | Line total |
|--------------------------------|-------------|--|------------|
| <input type="text" value="1"/> | D0CV0LL | 8,740.00 | 8,740.00 |
| Authorized User | Description | IBM ILOG CPLEX Optimization Studio Developer Edition Authorized User License + SW Subscription & Support 12 Months | |

- 90 Days Trial
- OPL Studio – Part of the distribution



Why OPL?

- OPL provides syntax that is close to the mathematical formulation, thus making it easier to make the transition from the mathematical formulation to something that can be solved by the computer.
- It enables a clean separation between the model and the accompanying data. The same model can then be solved with different input data with little extra effort.
- Other modeling languages: GAMS, AMPL and Mosel
- Used for linear and integer problems; not for non-linear problems!

Layout

The screenshot displays the IBM ILOG CPLEX Optimization Studio interface. The main window shows the CPLEX model code for a vehicle routing problem. The code is organized into sections: Given Sets, Parameters, and Decision Variables.

```
range Stops = 1..N; //bus stops
7
8//Given Sets
9 int Fast_Stops[Stops] = ...; //1 if the dwelling time is less than 20s; 0 otherwise
10 float T[Stops] = ...; //dwelling time in hours
11 float fixed_cost[Stops] = ...; //Fixed cost of resources
12 float E[Stops] = ...; //energy consumption between stops
13
14//Parameters
15 int A_PFS = ...; //the cost of a charger for 50 kW
16 int A_TFS = ...; //
17 int A_DFS = ...; //
18 int M = 1000000; //large enough number (could be maximum power used)
19 int cost_energy_battery = ...; //cost of 1 kWh of battery
20 int number_of_buses = ...; //number of buses
21 float battery_UB = ...; //maximum capacity of the battery
22 int power_UB_Fast_Stop = ...; //upper bound of power given by charger (kW) at stops with dwe
23 int power_UB_Slow_Stop = ...; //upper bound of power given by charger (kW) at stops with dwe
24 int power_LB_Fast_Stop = ...; //lower bound of power given by charger (kW) at stops with dwe
25 int power_LB_Slow_Stop = ...; //lower bound of power given by charger (kW) at stops with dwe
26 float DFS_number = ceil(number_of_buses/4);
27 int U_DFS = ...;
28 int L_DFS = ...;
29 int U_TFS = ...;
30 int L_TFS = ...;
31
32//Decision Variables
33 dvar float+ battery_UB;
34 dvar float+ power[Stops]; //power charged at stop in kWh
35 dvar float+ power_before[Stops]; //power level before visiting stop i in kWh
36 dvar float+ power_after[Stops]; //power level after visiting stop i in kWh
37 dvar float+ power_used[Stops]; //maximum power provided by PFS kW
38 dvar boolean has_PFS[Stops]; //1 - if has PFS; 0 - otherwise
```

The right-hand side of the interface shows the Outline window, which lists the model's components: using CPLEX, Internal data (3), DFS_number: float, M: int, Stops: range, External data (19), A_DFS: int, A_TFS: int, A_PFS: int, cost_energy_battery: int, E: float[Stops], Fast_Stops: int[Stops], fixed_cost: float[Stops], L_DFS: int, L_TFS: int, N: int, number_of_buses: int, power_LB_Fast_Stop: int, power_LB_Slow_Stop: int, power_UB_Fast_Stop: int, power_UB_Slow_Stop: int, S: int, T: float[Stops], U_DFS: int, U_TFS: int, Decision variables (8), battery_UB: dvar float+, capacity_exceeded: dvar boolean[Stops], has_PFS: dvar boolean[Stops], power: dvar float+[Stops].

At the bottom, the Problems window is empty, and the Scripting log, Solutions, Conflicts, Relaxations, Engine log, Statistics, and Profiler windows are also visible.

Syntax

- **Data Declarations** – to define known parameters

- simple:

- `int c = 8;`

- set:

- `range Days = 1 .. 7;`

- from data file:

- ▶ in the model file:

- `{string} days[Days] = ...;`

- ▶ in the data file:

- `days = {"Monday", "Tuesday", ... , "Sunday"};`

- **Decision Variables** –

- `dvar float+ x;`

- `dvar boolean y;`

Syntax

- **Objective Function** –
minimize, maximize
maximize $6 * x$;
- **Constraints** –
subject to {
 forall(i,j in I)
 $x[i][j] \leq 10$;

 $\text{sum}(i,j \text{ in } I)x[i][j] * 5 == 65$;
};
- **Print** –
execute{writeln("x=", x);}

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Small Example

A company produces two products:

- doors
- windows

It has three production facilities with limited production time available:

- Factory 1 produces the metal frame
- Factory 2 produces the wooden frame
- Factory 3 produces glass and mounts the parts

The products are produced in series of 200 items and each series generates a revenue depending on the product. Each series require a given amount of time of each factory's capacity. The problem is to find the number of series of each product to maximize the revenue.

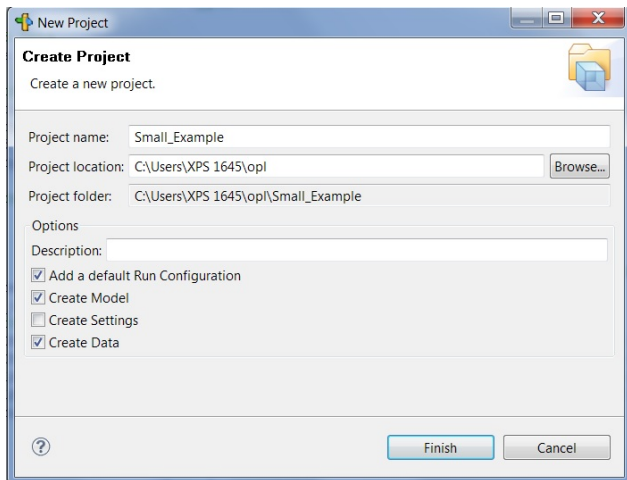
Small Example

| | Hours/Series | | Hours at Disposal |
|----------------|--------------|--------|-------------------|
| | Door | Window | |
| Factory 1 | 1 | 0 | 4 |
| Factory 2 | 0 | 3 | 12 |
| Factory 3 | 3 | 2 | 18 |
| Revenue/Series | 3 000 | 5 000 | – |

Small Example

- Formulate the problem mathematically:
 - input parameters
 - decision variable(s)
 - objective function
 - constraints
- Model the problem in OPL
- Run the model and check your results in the "Solutions" tab
- When finished proceed to the instructions 8 file

Create New Project in OPL

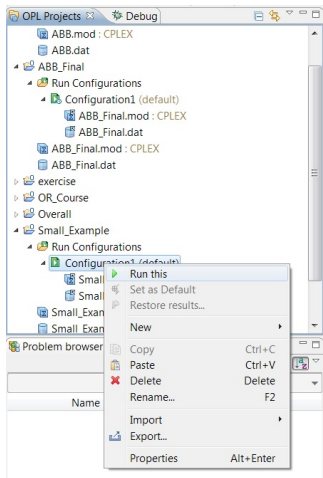


The screenshot shows a 'New Project' dialog box with the following fields and options:

- Project name:** Small_Example
- Project location:** C:\Users\XPS 1645\opl (with a 'Browse...' button)
- Project folder:** C:\Users\XPS 1645\opl\Small_Example
- Options:**
 - Add a default Run Configuration
 - Create Model
 - Create Settings
 - Create Data

At the bottom, there is a help icon (?), a 'Finish' button, and a 'Cancel' button.

How to Run the Model



Results

- Decision is integer:
 - revenue – 29 000
 - $x = [3 \ 4]$
- Decision is float:
 - revenue – 30 000
 - $x = [3.3333 \ 4]$

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References



- The presentation has been based on the following tutorial:
- http://folk.uio.no/trulsf/opl/opl_tutorial.pdf