Theoretical foundations Microeconomic consumer theory

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Introduction to choice models



The case of continuous goods

Continuous choice set

Consumption bundle

$$Q = \begin{pmatrix} q_1 \\ \vdots \\ q_J \end{pmatrix} p = \begin{pmatrix} p_1 \\ \vdots \\ p_J \end{pmatrix}$$

Budget constraint

$$p^T Q = \sum_{\ell=1}^J p_\ell q_\ell \leq I.$$

No attributes, just quantities and prices

Choice

Solution of an optimization problem

 $\max_{Q} \ \widetilde{U}(Q)$

subject to

 $p^T Q \leq I, \ Q \geq 0.$

Demand function

- Solution of the optimization problem
- Quantity as a function of prices and budget

 $Q^* = \operatorname{demand}(I, p)$

Example: Cobb-Douglas

$$\widetilde{U}(Q) = heta_0 \prod_{\ell=1}^J q_\ell^{ heta_\ell}$$

Example: Cobb-Douglas



Example



 q_1