



EXERCISES SESSION 12

This session focuses on *mixture models*, for which different model specifications are provided for the *Swissmetro* case study. Since Monte-Carlo integration is normally used when estimating mixtures of choice models, we refer the student to <http://biogeme.epfl.ch/documentation/montecarlo.pdf> for complete explanations.

First, download the file `Mixtures.zip`. It contains:

1. the base model `Base_Model.py`,
2. an heteroskedastic model `Mixture_Heteroskedastic.py`,
3. a model with random coefficients `Random_Coefficients.py`,
4. a mixed GEV model `Mixed_GEV.py`,
5. the file `Mixtures.SM.pdf` containing the description and interpretation of the different mixture models, and
6. the data file `swissmetro.dat`.

In the context of discrete choice models, mixture models are used to capture correlation among alternatives, alternative specific variances, taste heterogeneity, etc. In the following, you will see different specifications addressing them.

Base model The file `Base_model.py` contains the base model and is provided as a benchmark for comparison.

Heteroskedastic model The file `Mixture_Heteroskedastic.py` contains the heteroskedastic model. In this specification, we assume that the ASCs (ASC_{car} and ASC_{SM}) are randomly distributed with mean $\bar{\alpha}_{car}$ and $\bar{\alpha}_{SM}$ and standard deviation σ_{car} and σ_{SM} , respectively.

Error component model Now, copy the `Base_Model.py` file and use it as a template to perform the following tasks. Get inspiration from the heteroskedastic model to define the random terms.

1. Estimate an error component model in which the train and SM modes share the random term ζ_{rail} , which is assumed to be normally distributed. Fix the mean m_{rail} to zero and estimate the standard deviation σ_{rail} . You can call this file `Error_Component_01.py`.

2. Estimate an error component model in which car and train share the random term $\zeta_{existing}$ and train and SM share the random term ζ_{rail} . Both are assumed to be normally distributed. As before, the standard deviations $\sigma_{existing}$ and σ_{rail} need to be estimated, while the means $m_{existing}$ and m_{rail} are fixed to zero. You can call this file `Error_Component_02.py`.

Random coefficients model For this specification the base model is modified by defining alternative-specific coefficients for the cost of all alternatives. The model in which the parameters β_{car_cost} , β_{train_cost} , β_{SM_cost} and β_{he} are assumed to be randomly distributed over the population is provided in the file `Random_Coefficients.py`.

Mixed GEV models In this example we capture the substitution patterns by means of a nested logit model. We consider the model developed in `Random_Coefficients.py` in order to define a nested logit model. The resulting model is included in `Mixed_GEV.py`.

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