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# **Optimization and Simulation**

## **Simulation Exercise 5: Simulated Annealing**

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May 14, 2012

# The Exercise: Simulated Annealing

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- 5.1: Simulated Annealing for smooth optimization
- 5.2: Simulated Annealing for combinatorial optimization problem  
[Travelling salesman problem]
  - 5.2.1: Solution proposal function
  - 5.2.2: Objective function
  - 5.2.3: Putting the pieces together

# 5.1 Simulated Annealing for Smooth Optimization

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- Implement the function `SimulatedAnnealing.m` using the description
- Test your implementation with `SimulatedAnnealingTestSmooth.m`
  - Investigate the effect of different parameters
  - Try your own objective function

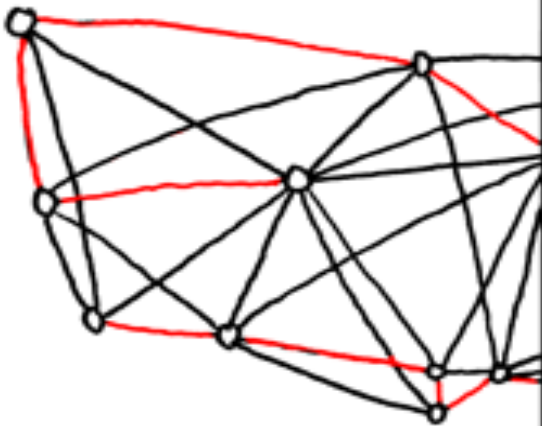
## 5.2 Travelling Salesman Problem

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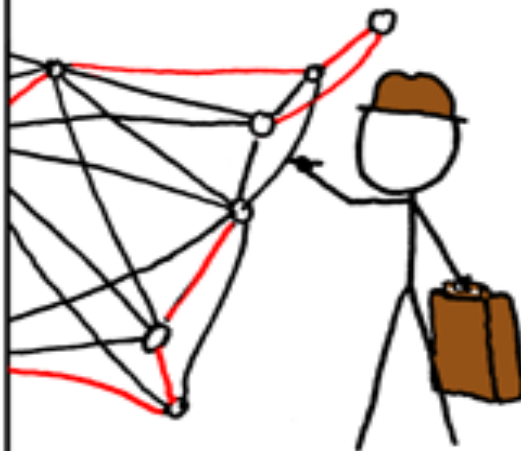
- A salesman has to visit  $n$  cities
  - He starts and ends his trip at his home city
  - Assume cost of travel to be total trip length
- What sequence of cities minimizes the travel cost?
  - Formulated in 1930s
  - Application: planning, logistics, manufacturing
  - NP-Hard problem
  - Approximate solutions

## 5.2 Travelling Salesman Problem

BRUTE-FORCE  
SOLUTION:  
 $O(n!)$



DYNAMIC  
PROGRAMMING  
ALGORITHMS:  
 $O(n^2 2^n)$



SELLING ON EBAY:  
 $O(1)$

STILL WORKING  
ON YOUR ROUTE?

SHUT THE  
HELL UP.



[www.xkcd.com](http://www.xkcd.com)

## 5.2 Travelling Salesman Problem

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- Cities are consecutively numbered:  $1, 2, \dots, N$
- We encode solutions as  $x = (x_1 x_2 \dots x_N)$  where
  - $x_i$  is the index of  $i^{th}$  city visited along the way
  - $x_N$  is the last city visited before returning home
  - Every city must be visited exactly once

## 5.2.1 Solution Proposal Function

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- Implement `RandomizeCitySequence.m`
- Test with `RandomizeCitySequenceTest.m`

## 5.2.2 Objective Function

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- Implement `EvaluateCitySequence.m`
- Test with `EvaluateCitySequenceTest.m`



## 5.2.3 Putting the Pieces Together

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- Run `SimulatedAnnealingTestTSP.m`
  - You already have the components ready
  - Try to reach the global optimum