
Spatial tessellations of pedestrian dynamics

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Content

- Interest & Motivation
- Related work
- Methodology
- Preliminary results
- Conclusions and future work

Interest & motivation

- Mathematical framework for detailed characterization of pedestrian flow indicators
- Understanding and predicting pedestrian flows
 - Efficient design of new facilities
 - Large events gathering a high number of people
 - Travel guidance
 - Congestion

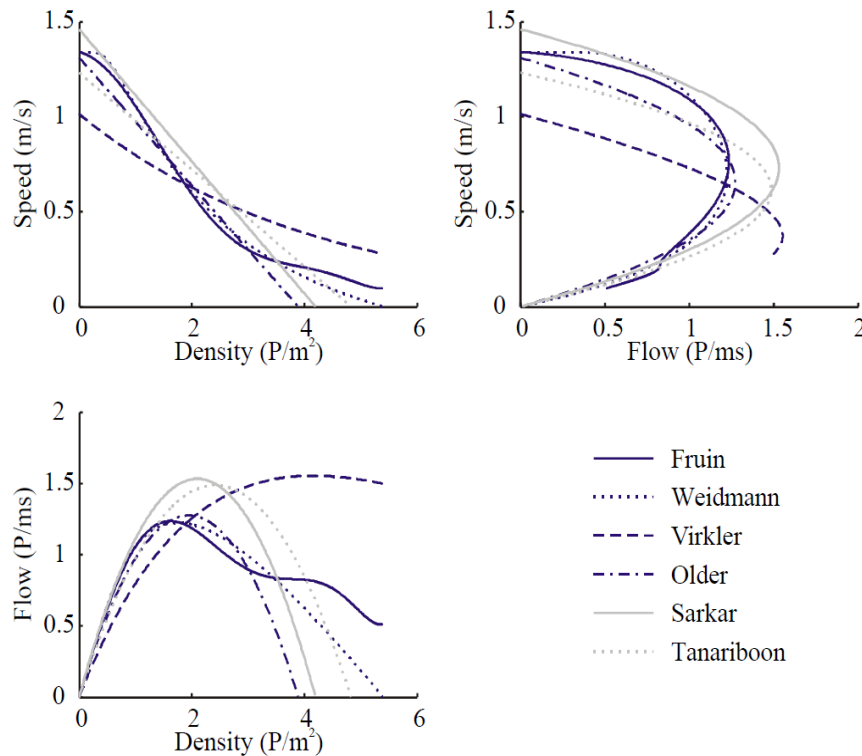
Lausanne railway station



Related work 1/2

- Models of pedestrian flow and behavior
 - Social force model (Helbing and Molnár, 1995)
 - Continuum model (Hughes, 2002)
 - Cellular automata (Blue and Adler, 2001)
- Empirical studies
 - Collective effects and self-organization phenomena
 - (Navin and Wheeler, 1969; Daamen and Hoogendoorn, 2003; Helbing et al., 2007; Schadschneider et al., 2008)
 - Quantitative analyses of pedestrian flow characteristics
 - (Fruin and Strakosch, 1987; Lam and Cheung, 2000; Helbing et al., 2001; Kretz et al., 2006; Wong et al., 2010; Rastogi et al., 2013)
 - Fundamental diagram
 - (Schadschneider et al., 2008; Zhang, 2012)

Related work 2/2



Contradictory empirical data base

Complex nature of pedestrian interactions

External factors

Social and psychological aspects

Different types of facilities

Different types of pedestrian flow

Measurement methods

Source: (Daamen et al., 2005)

Data collection



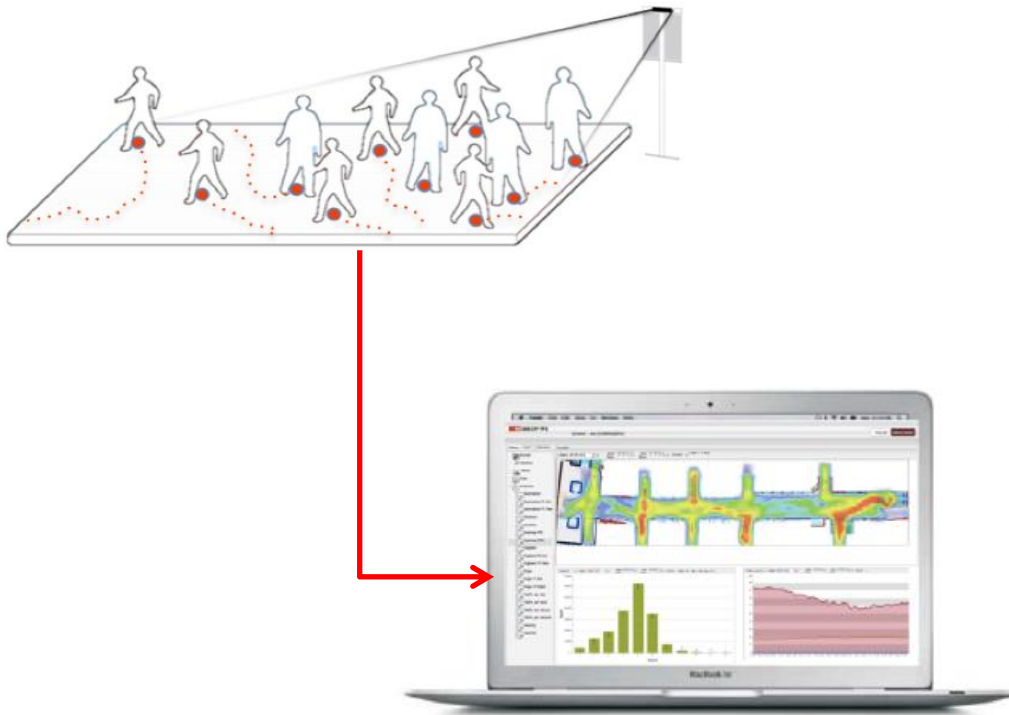
Source: (Alahi et al., 2013)

Case study: Gare de Lausanne

Depth sensors based pedestrian tracking

Vision processing outcome
($t, x(t), y(t), pedestrian_{id}$)

Data potential



- Pedestrian flow characteristics
- Pedestrian behavior
 - Interaction with moving and static objects
 - Collective behavior
 - Self-organization of pedestrian groups

Model calibration and validation

Flow characteristics

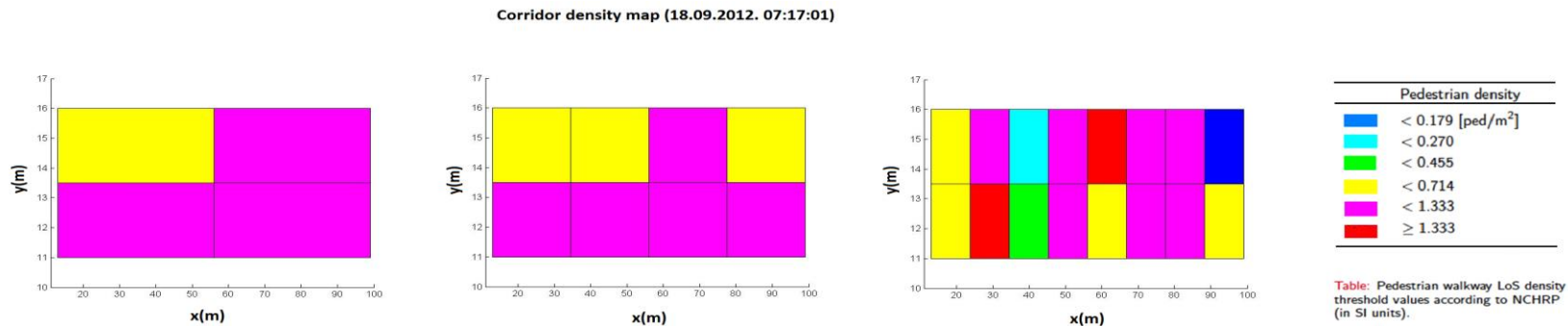
- Density (k) – number of pedestrians present at some instant per unit of space
- Flow (q) – number of pedestrians passing a fixed cross-section per unit of time
- Speed
 - Space mean speed (v_s) - average speed of pedestrians at some instant per unit of space
 - Time mean speed (v_t) - average speed of pedestrians passing through a given point per unit of time

Fundamental diagram: $q = v_s \cdot k$

Grid space representation

Density map

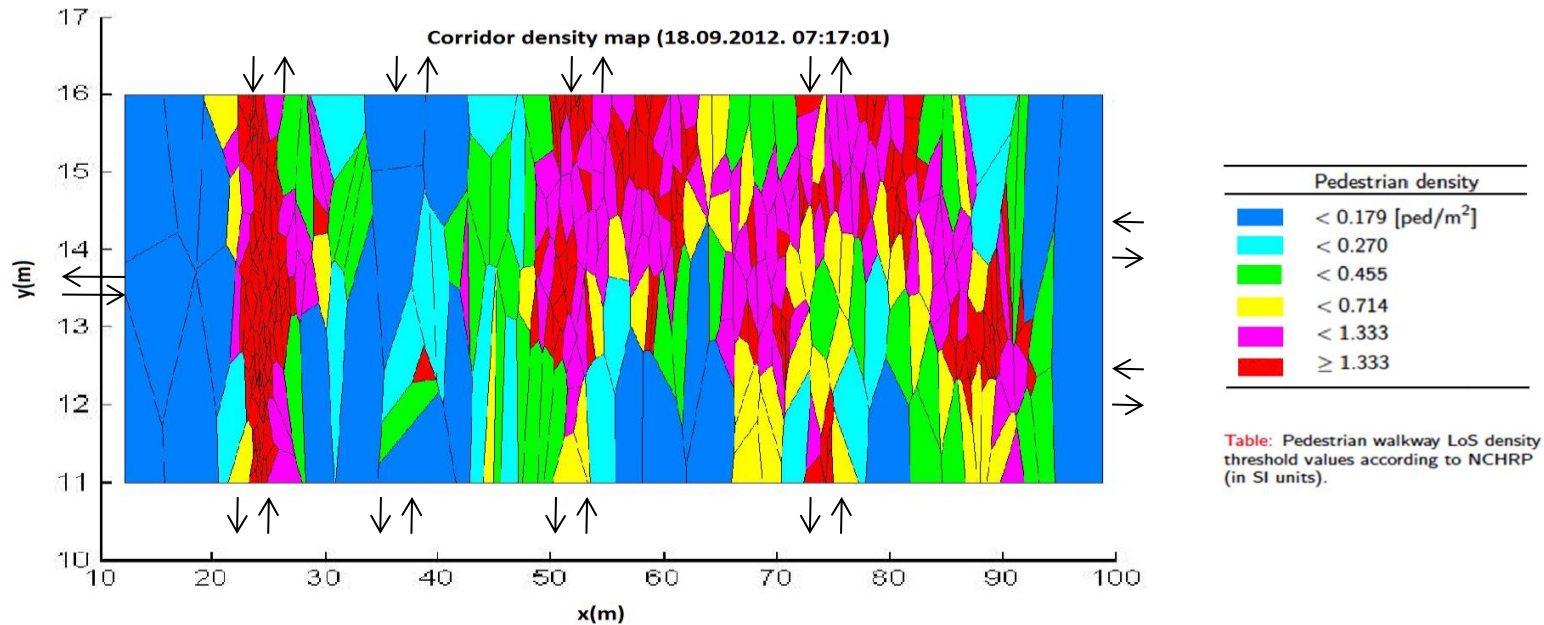
- The grid based method transforms the space into cell regions
 - Each cell - entirely homogenous



- Cell sizes: 2.5m × 43m, 2.5m × 21.5m, 2.5m × 10.75m
- *Modifiable areal unit problem*

Voronoi space representation

Density map



- Voronoi cell

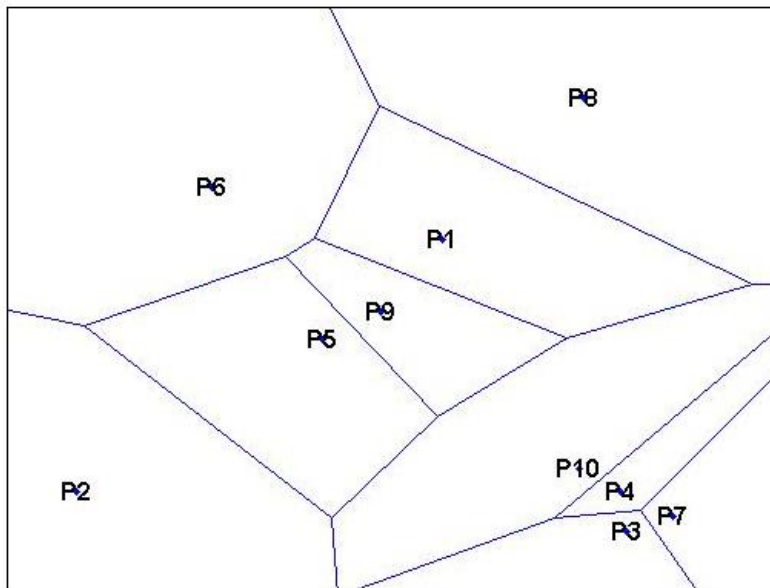
$$- V(p_i) = \{p \mid \|p - p_i\| \leq \|p - p_j\|, i \neq j\}$$

- Voronoi diagram

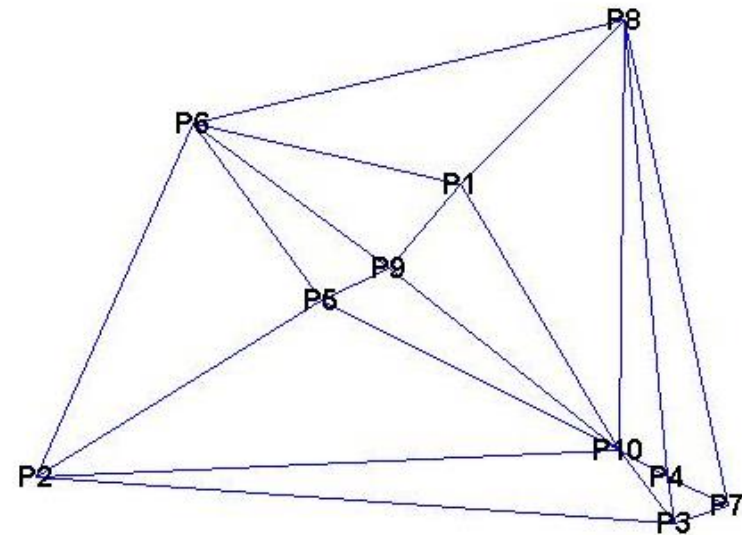
$$- V = \{V(p_1) \cap RoI, V(p_2) \cap RoI, \dots, V(p_n) \cap RoI\}$$

Merging cells

- Issue: small polygons allocated to pedestrians in very dense areas
 - Clustering based on Delaunay triangulation $d(p_i, p_j) < \delta, \forall i, j$
 - Weight associated to the corresponding space w_i

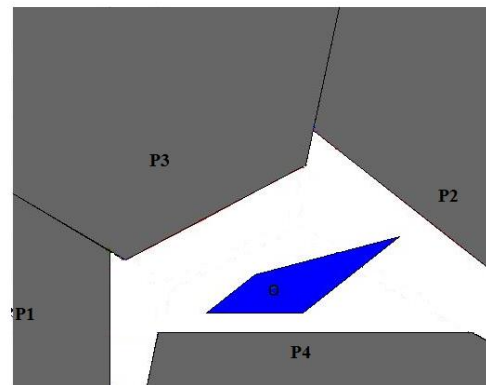
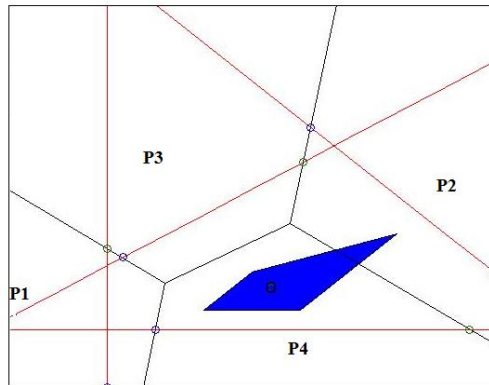
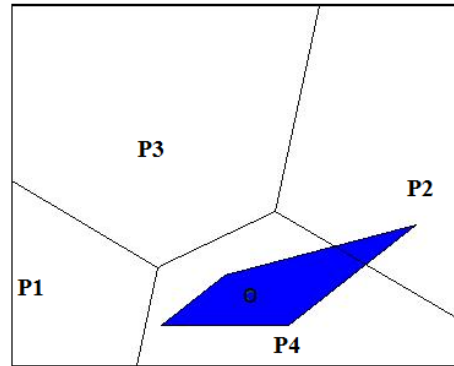
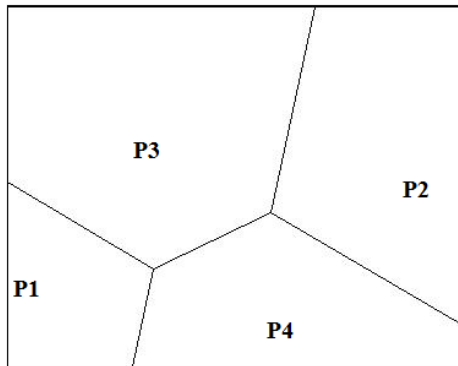


Voronoi diagram



Delaunay triangulation

Dealing with obstacles



Voronoi assumption

- It is possible to connect two generator points by a straight line

Voronoi diagram for points & Voronoi diagrams for areas

$$d(p_i, O) = \min_{o_j} \{ \|p_i - o_j\| \mid o_j \in O \}$$

Pedestrian flow indicators

- Space-time representation

$$p_i = (x_i, y_i, t_i)$$

- Density

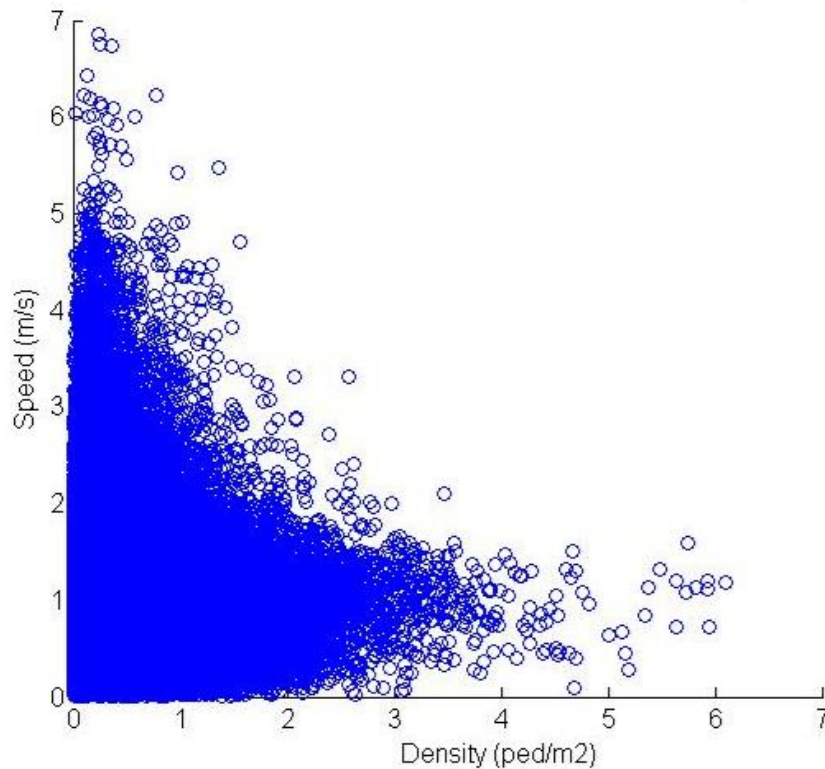
$$k(p_i) = \frac{w_i}{|V(p_i)|}$$

- Speed

$$v_s(p_i) = \frac{\|p_i(t_i - \Delta t) - p_i(t_i + \Delta t)\|}{2 \cdot \Delta t}, \Delta t = 0.5s$$

w_i - weight corresponding to the group of pedestrians

Empirical speed-density relationship



Density

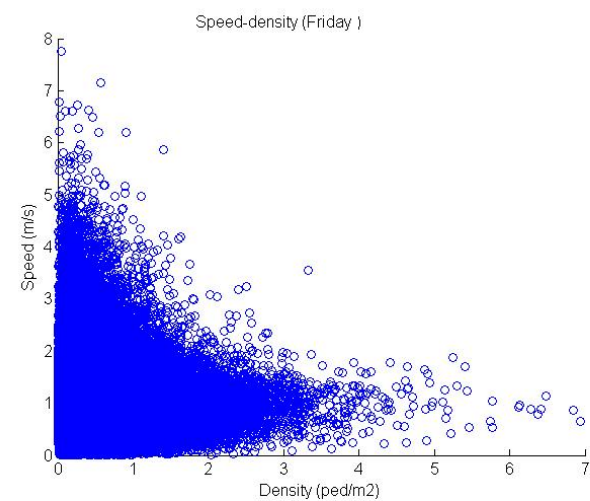
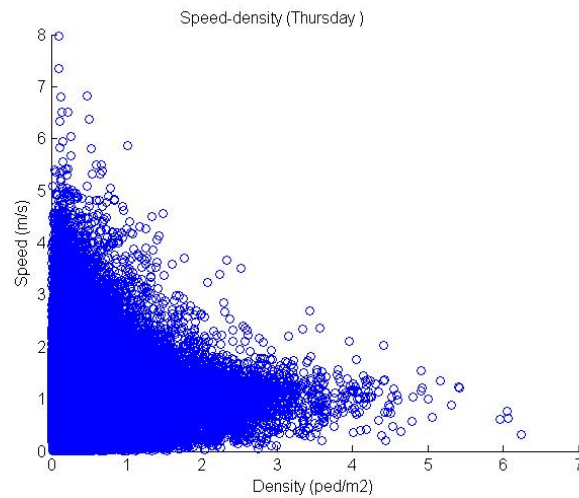
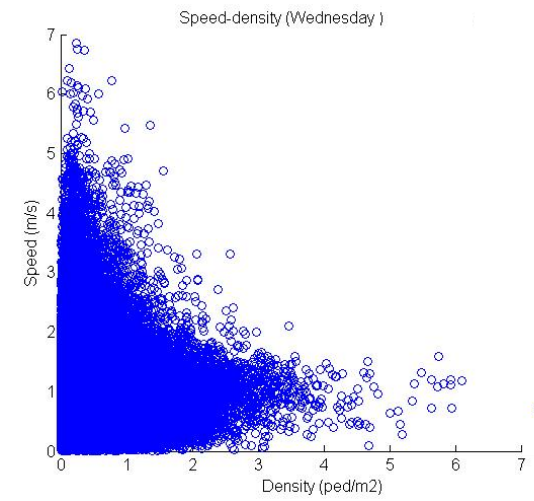
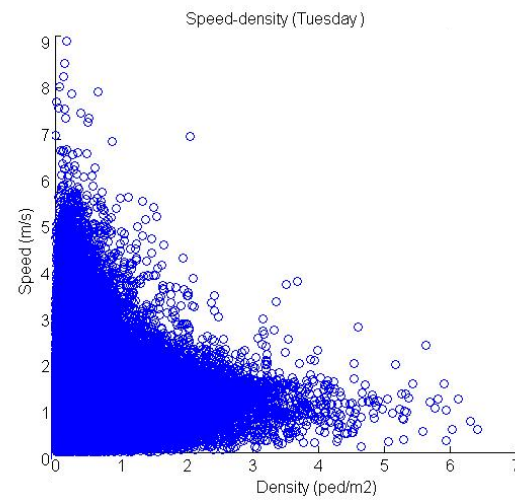
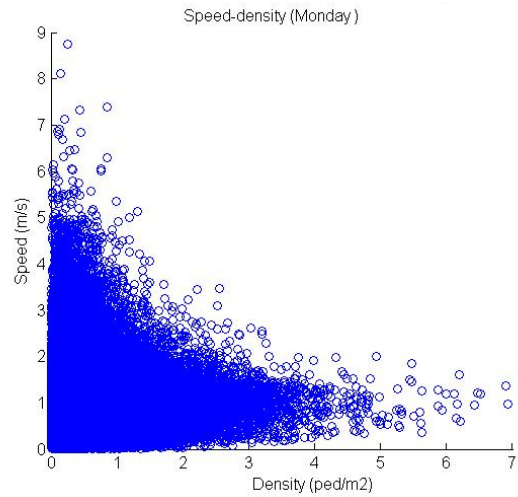
$$k(p_i) = \frac{w_i}{|V(p_i)|}$$

Speed

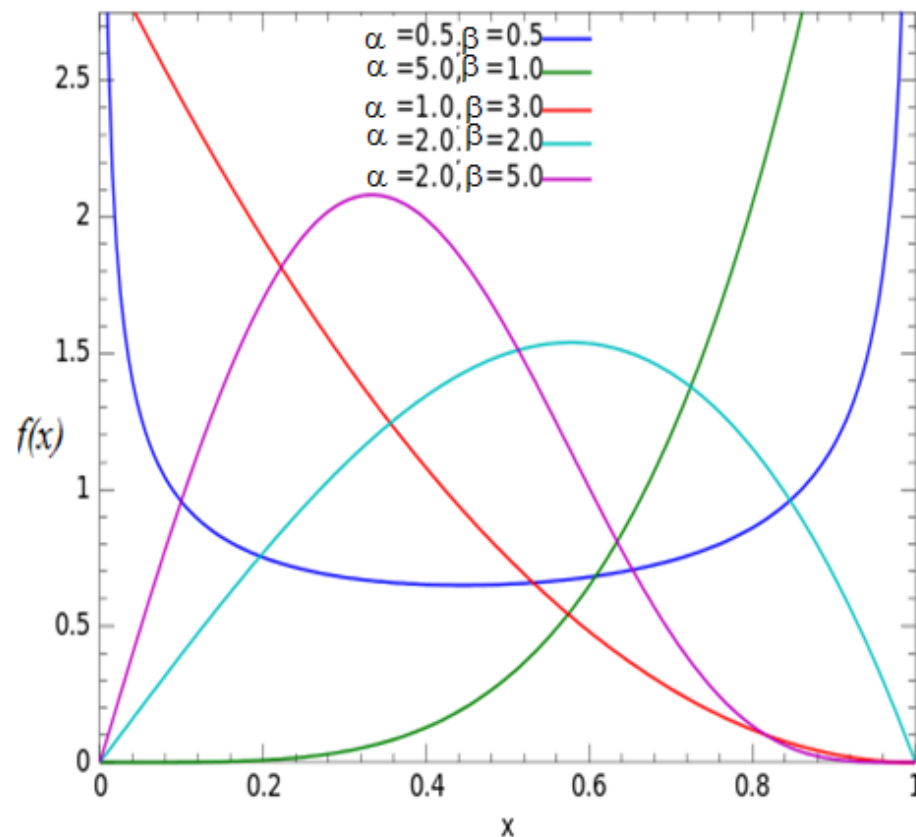
$$v_s(p_i) = \frac{\|p_i(t_i - \Delta t) - p_i(t_i + \Delta t)\|}{2 \cdot \Delta t}$$

$$\Delta t = 0.5s$$

Speed-density profiles



Kumaraswamy distribution

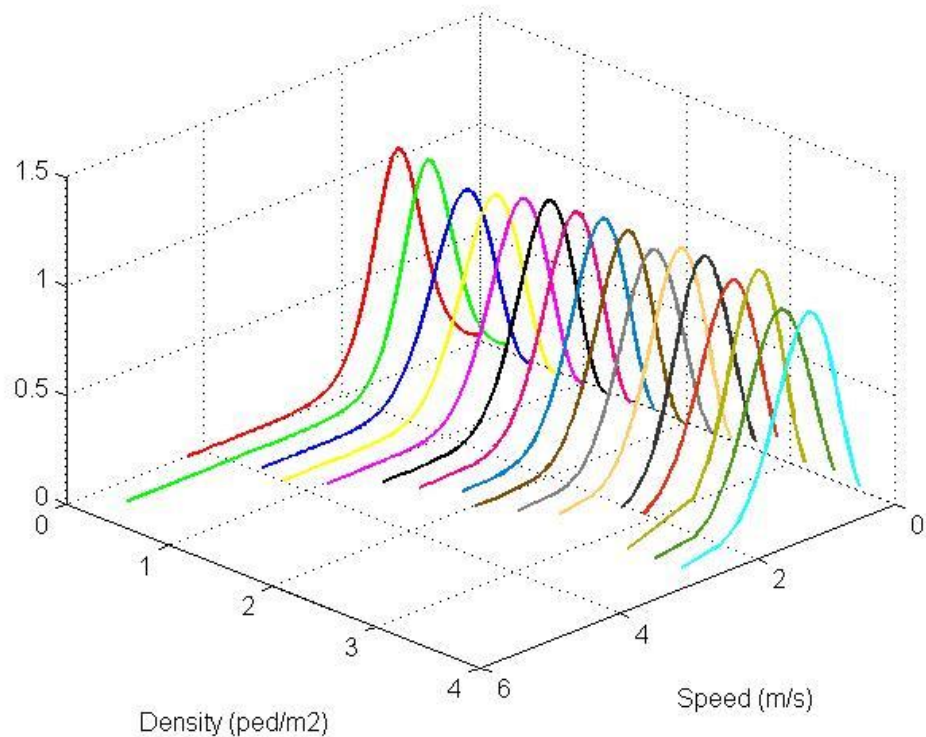


- Defined on the bounded region $[l, u]$
- Two non-negative shape parameters α and β
- The simple closed form of pdf $f(x)$ and cdf $F(x)$

$$f(x) = \frac{\alpha \cdot \beta \cdot (x-l)^{\alpha-1} \cdot ((u-l)^\alpha - (x-l)^\alpha)^{\beta-1}}{(u-l)^{\alpha\beta}}$$

$$F(x) = 1 - \left(1 - \left(\frac{x-l}{u-l}\right)^\alpha\right)^\beta$$

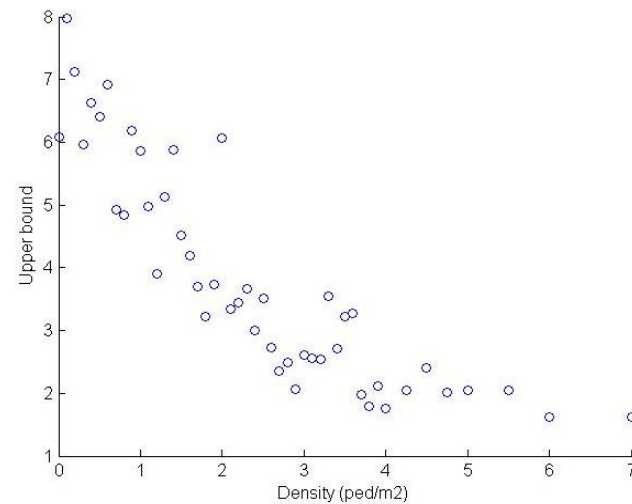
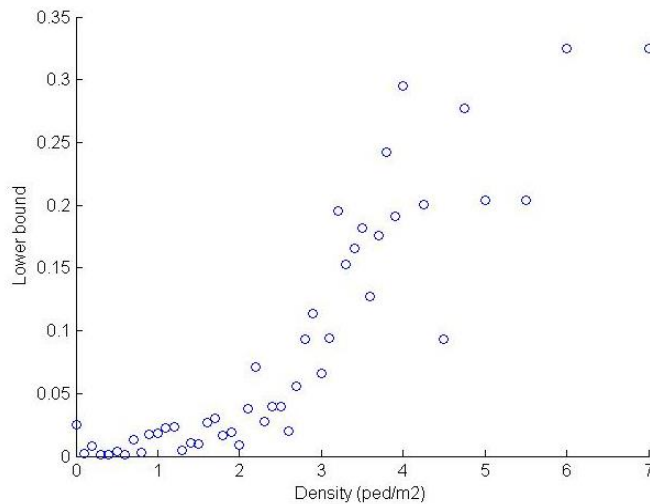
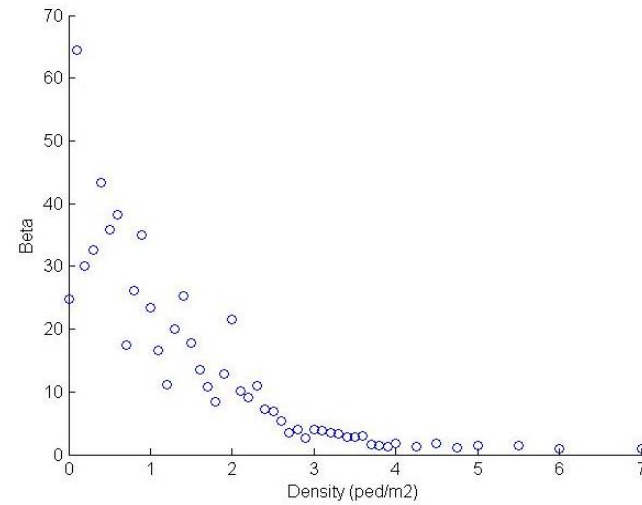
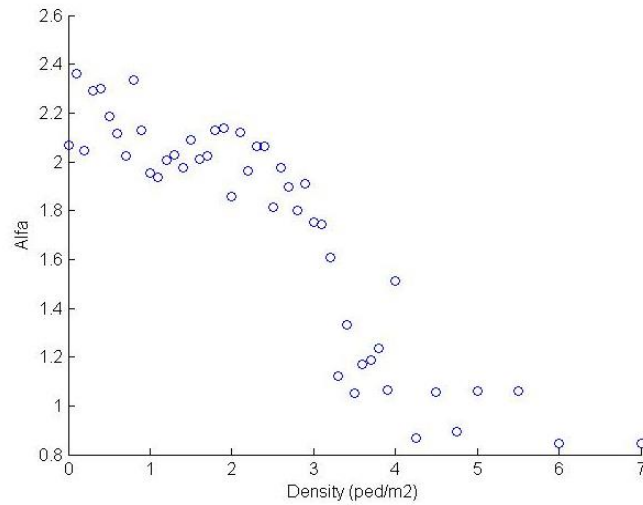
Probabilistic speed-density relationship



$$V \sim f(\alpha(k), \beta(k), l(k), u(k))$$

- f – Kumaraswamy *pdf*
- V – speed
- k – density level
- α, β – shape parameters
- l, u – boundary parameters

Parameters specification



Model specification

- Speed-density relationship

$$V \sim f(\alpha(k), \beta(k), l(k), u(k))$$

Parameter	Specification 1	Specification 2
$\alpha(k)$	$a_\alpha k^3 + b_\alpha k^2 + c_\alpha k + d_\alpha$	$a_\alpha k^3 + b_\alpha k^2 + c_\alpha k + d_\alpha$
$\beta(k)$	$a_\beta \exp(b_\beta k)$	$a_\beta \exp(b_\beta k)$
$u(k)$	$a_u \exp(b_u k)$	$a_u k^3 + b_u k^2 + c_u k + d_u$
$l(k)$	0	0

Model estimation

- Maximum log-likelihood

$$\log \mathcal{L} = \sum_{i=1}^n \log(\alpha(k_i)) + \sum_{i=1}^n \log(\beta(k_i)) + \sum_{i=1}^n (\alpha(k_i) - 1) \log(v_i - l(k_i)) + \sum_{i=1}^n (\beta(k_i) - 1) \log\left(\frac{u(k_i) - l(k_i)}{(v_i - l(k_i))^{\alpha(k_i)} - (v_i - l(k_i))^{\alpha(k_i)})}\right) - \sum_{i=1}^n \alpha(k_i) \beta(k_i) \log(u(k_i) - l(k_i))$$

$$u(k_i) \leq \max(v_i), i = 1, \dots, n$$

	a_α	b_α	c_α	d_α	a_β	b_β	a_u	b_u	c_u	d_u	LL
Specification 1	0.248	-0.6968	0.1603	2.2452	68.894	-0.8751	8.0608	-0.2833			-1.6497e+05
Specification 2	0.0498	-0.2823	-0.0207	2.0089	45.362	-0.5945	0.0002	-0.0002	-0.0010	8.0017	-1.699372e+05

Conclusion

- High data potential
 - Detailed pedestrian flow studies
- Voronoi representation of space
 - Good space resolution
 - Reveals phenomenon not observable with the other methods
- Pedestrian oriented definitions of flow indicators
- Probabilistic speed-density relationship

Future work

- Validation of the speed-density model
- Time discretization
 - Consistent with the philosophy of space decomposition
- Definition of flow indicator

THANK YOU

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