

# Decision-Aid Methodologies in Transportation

## Introduction to Choice Models

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# Outline

- 1 Introduction
- 2 Simple example
- 3 Model

# Modeling behavior

- Individual behavior (vs. aggregate behavior)
- Theory of behavior which is:
  - **mostly descriptive and not too prescriptive**: how people behave and not how they should;
  - **general**: not too specific;
  - **operational**: can be used in practice for forecasting.
- Type of behavior: **discrete choice**, i.e. what is observed is a discrete action

# Motivations

## Field :

- ▶ Marketing
- ▶ Transportation
- ▶ Politics
- ▶ Management
- ▶ New technologies
- ▶ Finance
- ▶ Health
- ▶ etc.

## Type of behavior:

- ▶ Choice of a brand
- ▶ Choice of a transportation mode
- ▶ Choice of a representative
- ▶ Choice of a management policy
- ▶ Choice of investments
- ▶ Choice of portfolios of assets
- ▶ Choice of treatment

# Importance

Daniel McFadden



- UC Berkeley 1963, MIT 1977, UC Berkeley 1991;
- Laureate of *The Bank of Sweden Prize in Economic Sciences in Memory of Alfred Nobel, 2000*;
- Owns a farm and vineyard in Napa Valley;
- “Farm work clears the mind, and the vineyard is a great place to prove theorems”.

# Simple example

## Travel Information System (TIS):

- What is the market penetration?
- How will the penetration change in the future?
- Assumption: level of education is an important explanatory factor.

## Data collection:

- Sample of 600 persons, randomly selected;
- Two questions:
  - 1 Do you subscribe to a travel information system? (yes/ no)
  - 2 How many years of education have you had? (low/ medium/ high)

# Simple example (cont.)

- Contingency table

TIS	Education			
	Low	Medium	High	
Yes	10	100	120	230
No	140	200	30	370
	150	300	150	600

- Penetration in the sample:  $230/600 = 38.3\%$
- Forecasting: need for a model

## Example: A model

- Dependent variable:

$$y = \begin{cases} 1 & \text{if subscriber} \\ 2 & \text{if not subscriber} \end{cases}$$

Discrete dependent variable

- Independent or explanatory variable

$$x = \begin{cases} 1 & \text{if level of education is low} \\ 2 & \text{if level of education is medium} \\ 3 & \text{if level of education is high} \end{cases}$$

## Example: Probabilities

### Marginal probability

- frequency of subscribing in the population
- $\hat{p}(y = 1) = 10/600 + 100/600 + 120/600 = 0.383$
- Market penetration in population:  $p(y = 1)$  inferred from sample market penetration  $\hat{p}(y = 1)$

### Joint probability

- frequency of subscribing and medium level of education
- $\hat{p}(y = 1, x = 2) = 100/600 = 0.1667$

### Conditional probabilities

- frequency of subscribing among people with medium level of education
- $\hat{p}(y = 1|x = 2) = \hat{p}(y = 1, x = 2)/\hat{p}(x = 2) = 0.167/0.5 = 0.33$

## Example: Probabilities (cont.)

Similarly, we obtain:

$$\hat{p}(y = 1|x = 1) = 0.067$$

$$\hat{p}(y = 1|x = 2) = 0.333$$

$$\hat{p}(y = 1|x = 3) = 0.8$$

We assume a causal relationship.

**Interpretation** → level of education explains subscription propensity

- Behavioral model:  $\hat{p}(y = i|x = j)$
- Forecasting assumption: stable over time

# Example: Forecasting

- Model:

$$p(y = 1|x = 1) = \pi_1 = 0.067$$

$$p(y = 1|x = 2) = \pi_2 = 0.333$$

$$p(y = 1|x = 3) = \pi_3 = 0.8$$

where  $\pi_1, \pi_2, \pi_3$  are estimated parameters.

- Assumption: future split of levels of education: 10%, 60%, 30%

Q: What is the future uptake of TIS ?

$$\begin{aligned} p(y = 1) &= \sum_{j=1}^3 p(y = 1|x = j)p(x = j) \\ &= 0.1\pi_1 + 0.6\pi_2 + 0.3\pi_3 \\ &= 44.67\% \end{aligned}$$

## Example: Forecasting (cont.)

- If the level of education increases
  - from 25%, 50%, 25% to 10%, 60%, 30%,
- The market penetration of TIS will increase
- From 38.33 % to 44.67%.

In summary:

- $p(x = j)$  can be easily obtained and forecasted;
- $p(y = i|x)$  is the behavioral model to be developed.

# Model assessment





## Informal checks

- Do these estimates make sense?
- Do they match our a priori expectations?
- Here: as years of education increases, there is a higher propensity to subscribe to a travel information system.

## Quality of the estimates

- How is  $\hat{\pi}$  different from  $\pi$  ?
- We have no access to  $\pi$
- For each sample we would obtain a different  $\hat{\pi}$

# Bibliography

-  Ben-Akiva, M., Bierlaire, M., Walker, J. *Discrete Choice Analysis*. Draft chapters.
-  Ben-Akiva, M. and Lerman, S. R. (1985), *Discrete Choice Analysis: Theory and Application to Travel Demand*, MIT Press, Cambridge, Ma.
-  Train, K. (2003). *Discrete Choice Methods with Simulation*, Cambridge University Press.  
<http://emlab.berkeley.edu/books/choice.html>
-  Hensher, D., Rose, J., and Greene, W. (2005), *Applied choice analysis: A primer*, Cambridge University Press.