

Price Optimization

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Introduction

- Choice model captures demand
- Demand is elastic to price
- Predicted demand varies with price, if it is a variable of the model
- In principle, the probability to use/purchase an alternative decreases if the price increases.
- The revenue per user increases if the price increases.
- Question: what is the optimal price to optimize revenue?

In short:

- Price \uparrow \Rightarrow profit/passenger \uparrow and number of passengers \downarrow
- Price \downarrow \Rightarrow profit/passenger \downarrow and number of passengers \uparrow
- What is the best trade-off?

Revenue calculation

Number of persons choosing alternative i in the population

$$\hat{N}(i) = \sum_{s=1}^S N_s P(i|x_s, p_{is})$$

where

- p_s is the price of item i in segment s
- x_s gathers all other variables corresponding to segment s
- the population is segmented into S homogeneous strata
- $P(i|x_s, p_{is})$ is the choice model
- N_s is the number of individuals in segment s

Revenue calculation

The total revenue from i is therefore:

$$R_i = \sum_{s=1}^S N_s P(i|X_s, p_{is}) p_{is}$$

If the price is constant across segments, we have

$$R_i = p_i \sum_{s=1}^S N_s P(i|X_s, p_i)$$

Price optimization

Optimizing the price of product i is solving the problem

$$\max_{p_i} p_i \sum_{s=1}^S N_s P(i | x_s, p_i)$$

Notes:

- It assumes that everything else is equal
- In practice, it is likely that the competition will also adjust the prices

Illustrative example

A binary logit model with

$$\begin{aligned}V_1 &= \beta_p p_1 - 0.5 \\V_2 &= \beta_p p_2\end{aligned}$$

so that

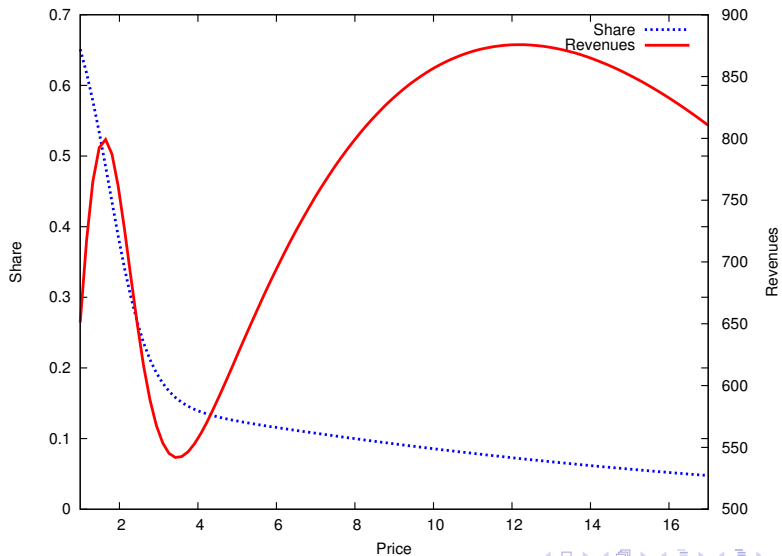
$$P(1|p) = \frac{e^{\beta_p p_1 - 0.5}}{e^{\beta_p p_1 - 0.5} + e^{\beta_p p_2}}$$

Two groups in the population:

- Group 1: $\beta_p = -2$, $N_s = 600$
- Group 2: $\beta_p = -0.1$, $N_s = 400$

Assume that $p_2 = 2$.

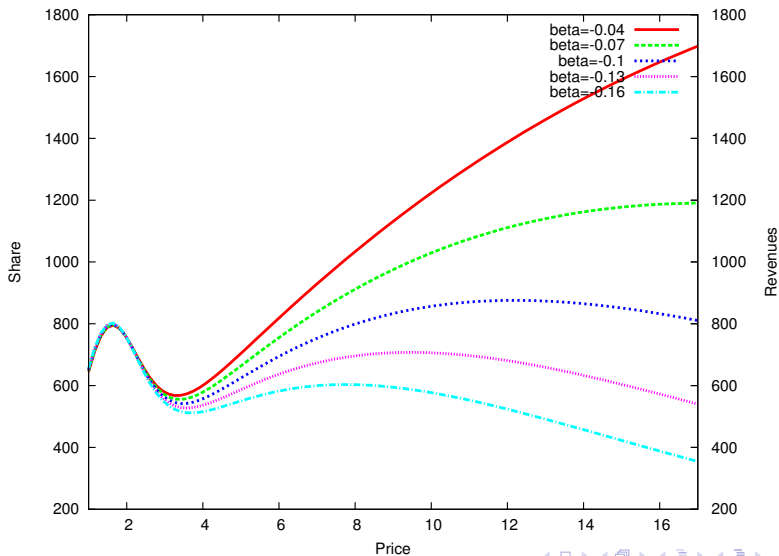
Illustrative example



Sensitivity analysis

- Parameters are estimated, we do not know the real value
- 95% confidence interval: $[\hat{\beta}_p - 1.96\sigma, \hat{\beta}_p + 1.96\sigma]$
- Perform a sensitivity analysis for β_p in group 2

Sensitivity analysis



Summary

Comments

- Typical non concavity of the revenue function due to taste heterogeneity.
- In general, decision making is more complex than optimizing revenues.
- Applying the model with values of x very different from estimation data may be highly unreliable.
- accounting for market organization and type of competition strongly affects the problem to model