Introduction to choice models

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Modeling behavior

- Individual behavior (vs. aggregate behavior)
- Theory of behavior which is
 - **descriptive**: how people behave and not how they should
 - abstract: not too specific
 - operational: can be used in practice for forecasting
- Type of behavior: choice





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Motivations

Field :

- Marketing
- Transportation
- Politics
- Management
- New technologies

Type of behavior:

- Choice of a brand
- Choice of a transportation mode
- Choice of a president
- Choice of a management policy
- Choice of investments





Importance

Daniel

L.

McFadden



1937–

- UC Berkeley 1963, MIT 1977, UC Berkeley 1991
- Laureate of The Bank of Sweden Prize in Economic Sciences in Memory of Alfred Nobel 2000
- Owns a farm and vineyard in Napa Valley
- "Farm work clears the mind, and the vineyard is a great place to prove theorems"





Travel Information System

- What is the market penetration?
- How will the penetration change in the future?
- Assumption: level of education is an important explanatory factor
- Data collection
 - sample of 600 persons, randomly selected
 - Two questions:
 - 1. Do you subscribe to a travel information system? (yes/no)
 - 2. How many years of education have you had? (low/medium/high)







• Contingency table

		Education		
TIS	Low	Medium	High	
Yes	10	100	120	230
No	140	200	30	370
	150	300	150	600

- Penetration in the sample: 230/600 = 38.3%
- Forecasting: need for a model





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Example: a model

Dependent variable:

 $y = \begin{cases} 1 & \text{if subscriber} \\ 2 & \text{if not subscriber} \end{cases}$

Discrete dependent variable

Independent or explanatory variable

- $x = \begin{cases} 1 & \text{if level of education is now} \\ 2 & \text{if level of education is medium} \\ 3 & \text{if level of education is high} \end{cases}$





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Example: a model

- Market penetration in the sample: $\hat{p}(y=1)$
- Market penetration in the population: p(y = 1) estimated by $\hat{p}(y = 1)$
- Joint probabilities: $\hat{p}(y = 1, x = 2) = 100/600 = 0.1667$
- Marginal probabilities: $\hat{p}(y=1) = \sum_{k=1}^{3} \hat{p}(1,k) = 10/600 + 100/600 + 120/600 = 0.383$
- Conditional probabilities: $\hat{p}(y = 1 | x = 2)$

$$\hat{p}(y = 1, x = 2) = \hat{p}(y = 1 | x = 2) \hat{p}(x = 2)$$

$$\hat{p}(y = 1 | x = 2) = \hat{p}(y = 1, x = 2) / \hat{p}(x = 2)$$

$$= 0.1667 / 0.5 = 0.333$$





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Similarly, we obtain

$$\hat{p}(y = 1 | x = 1) = 0.067$$

 $\hat{p}(y = 1 | x = 2) = 0.333$
 $\hat{p}(y = 1 | x = 3) = 0.8$

We obtain a causal relationship.

- Behavioral model: $\hat{p}(y = i | x = j)$
- Forecasting assumption: stable over time





• Model:

$$p(y = 1 | x = 1) = \pi_1 = 0.067$$

$$p(y = 1 | x = 2) = \pi_2 = 0.333$$

$$p(y = 1 | x = 3) = \pi_3 = 0.8$$

where π_1 , π_2 , π_3 are estimated parameters

• Assumption: future level of education: 10%-60%-30%

$$p(y = 1) = \sum_{i=1}^{3} p(y = 1 | x = i) p(x = i)$$

= 0.1\pi_1 + 0.6\pi_2 + 0.3\pi_3
= 44.67\%





Example: forecasting

- If the level of education increases
- from 25%-50%-25% to 10%-60%-30%
- Market penetration of TIS will increase
- from 38.33 % to 44.67%
- In summary
 - p(x = j) can be easily obtained and forecasted
 - p(y = i|x) is the behavioral model to be developed





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