EPFL ENAC TRANSP-OR **Prof. M. Bierlaire** 



Mathematical Modeling of Behavior Fall 2018

# LAB SESSION 9

The topic of this session is *Segmentation and tests*. You will estimate different model specifications for the *Airline Itinerary Choice* (Boeing) case study and you will go through some provided files to see how to test different specifications. The purposes of this lab are the following:

- improve the model specification with alternative-specific coefficients by adding some nonlinearities to the deterministic part of the utility function,
- test models whose hypothesis are non-nested, and
- improve the *Multinomial Logit* model by applying a socioeconomic segmentation.

First, download the .zip folder under Case Study 09. It contains:

- 1. the description and interpretation of the different models (09Description2018.pdf),
- 2. folder to develop the non linear specifications (NonLinear),
- 3. folder with the non nested specifications (NonNested), and
- 4. folder with the market segmentation (MarketSegmentation).

## Nonlinear specifications

For this part of the lab, copy the MNL\_airline\_specific.py file (included in the NonLinear folder) and use it as a template to perform the following tasks.

- 1. Try to code the proposed specifications. You should create the following files:
  - (a) MNL\_airline\_piecewise.py
  - (b) MNL\_airline\_powerseries.py
  - (c) MNL\_airline\_boxcox.py
- 2. Estimate the model specifications. You should obtain the following files:
  - (a) MNL\_airline\_piecewise.html
  - (b) MNL\_airline\_powerseries.html
  - (c) MNL\_airline\_boxcox.html
- 3. For each specification, perform a likelihood ratio test against the base model (MNL\_airline\_specific.py)
- 4. In order to verify that your code is correct, compare the results you obtain with the ones we provide in the description.

5. Can you use a likelihood ratio test to decide between models with different non-linearities?

## Non nested specifications

For this part of the lab, we provide all the required <code>.py</code> files and ask you to perform the following tasks.

- 1. Estimate the model specifications contained in the following files:
  - (a) MNL\_airline\_specific.py (Fare is considered linear)
  - (b) MNL\_airline\_log.py (Fare is considered logarithmic)
- 2. Results of the linear fare are already presented in the description document of the lab. For the logarithmic fare, you should obtain the file MNL\_airline\_log.html.
- 3. Perform a Cox-test between the model where the fare is considered linear and the one where it is considered logarithmic. To do so, run the model included in the file MNL\_airline\_composite.py. You should obtain the file MNL\_airline\_composite.html. What is the outcome of this test?

## Market Segmentation

For this part of the lab, we provide all the required .py files and we ask you to perform the following tasks.

- 1. Estimate the model specification contained in the file MNL\_airline\_specific.py. You should obtain the file MNL\_airline\_specific.html.
- 2. To test if there is a taste variation across segments, more precisely across gender, estimate the following models:
  - (a) MNL\_airline\_male.py (only for male)
  - (b) MNL\_airline\_female.py (only for female)
  - (c) MNL\_airline\_GenderNA.py (only for no answer for the gender variable)
- 3. You should obtain the following files:
  - (a) MNL\_airline\_male.html
  - (b)  $MNL_airline_female.html$
  - (c) MNL\_airline\_GenderNA.html
- 4. Perform a likelihood ratio test between the base model (MNL\_airline\_specific.py) and the *segmented* models (MNL\_airline\_male.py, MNL\_airline\_female.py and MNL\_airline\_GenderNA.py). What is the outcome of the test?

## Create and analyze

You can develop other model specifications using your own hypotheses. We suggest you to take MNL\_airline\_specific.py as the base model and then do the following:

1. Try a socioeconomic segmentation of the alternative specific constant, which is equivalent to adding socioeconomic parameters directly to the utilities. Is this segmentation significant? 2. Try a socioeconomic segmentation of attributes of the alternatives one-by-one. Remember the difference between discrete and continuous segmentations. Are your segmentations significant?

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